

# Oscillations of non-slender tori in the Hartle-Thorne geometry

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# Goals

## What?

- ▶ To examine the influence of quadrupole moment of neutron stars on the oscillation frequencies of accretion tori.

## Why?

- ▶ To use in modeling kHz QPO observed in power spectra of low-mass X-ray binaries containing a neutron star.

# Previous research

## Abramowicz et al. 2003

- ▶ Epicyclic frequencies of free test particles in Hartle-Thorne geometry.

## Straub and Šrámková 2009

- ▶ Pressure corrections on epicyclic frequencies of oscillating tori in Kerr geometry.

# Spacetime geometry around neutron stars

## Hartle-Thorne metric<sup>1</sup>

$$ds^2 = g_{tt}dt^2 + 2g_{t\varphi}dtd\varphi + g_{rr}dr^2 + g_{\theta\theta}d\theta^2 + g_{\varphi\varphi}d\varphi^2,$$

$$g_{tt} = - \left( 1 - \frac{2M}{r} \right) [1 + j^2 F_1(r) + q F_2(r)],$$

$$g_{rr} = \left( 1 - \frac{2M}{r} \right)^{-1} [1 + j^2 G_1(r) - q F_2(r)],$$

$$g_{\theta\theta} = r^2 [1 + j^2 H_1(r) + q H_2(r)],$$

$$g_{\varphi\varphi} = r^2 \sin^2 \theta [1 + j^2 H_1(r) + q H_2(r)],$$

$$g_{t\varphi} = - \frac{2M^2}{r} j \sin^2 \theta.$$

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<sup>1</sup>Abramowicz et al. 2003.

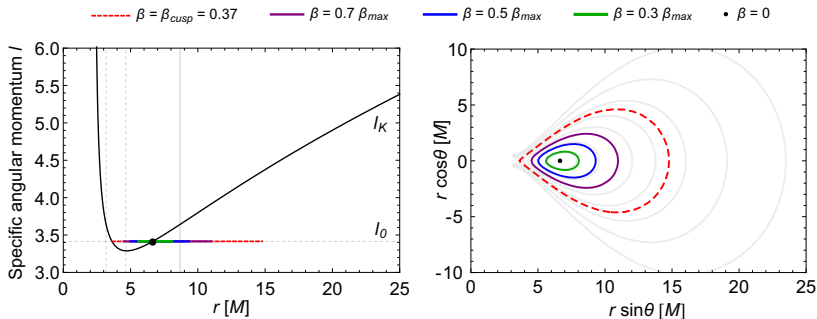
# Torus model<sup>2</sup>

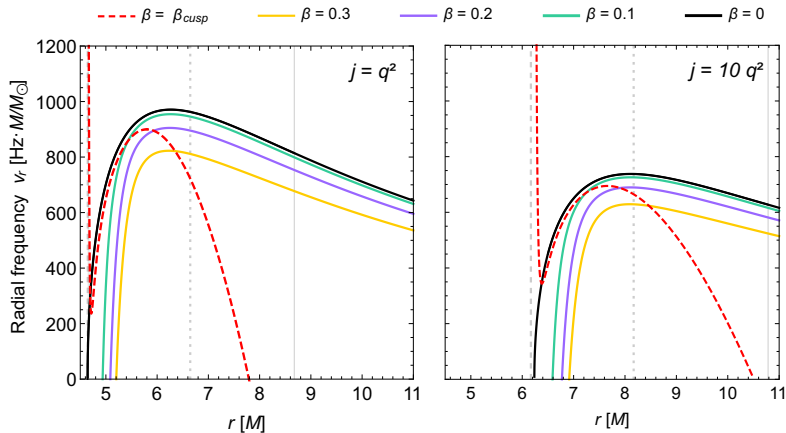
- ▶ Perfect polytropic fluid.
- ▶ Stationary flow.
- ▶ Fluid in a state of pure rotation.
- ▶ Constant specific angular momentum.
- ▶ Non-self-gravitating.

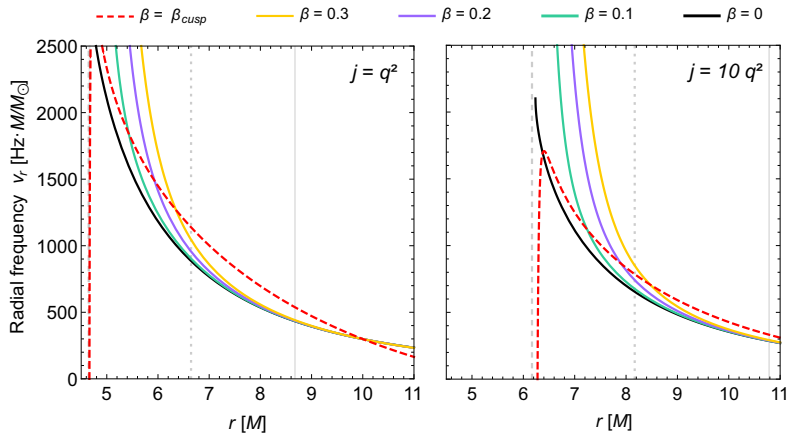
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<sup>2</sup>Abramowicz et al. 2006.

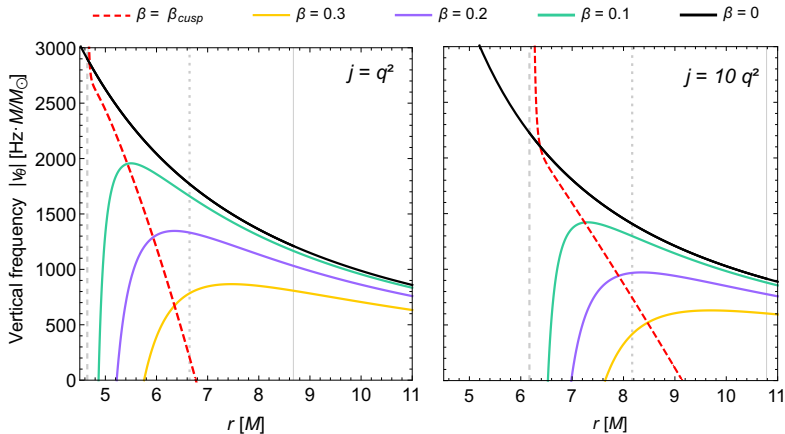
# Torus construction



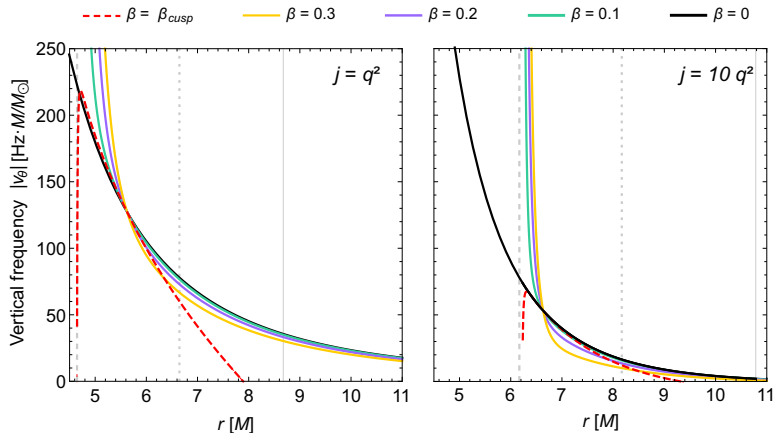
Radial oscillation,  $m = 0$ ,  $j = 0.4$ 

Radial oscillation,  $m = -1$ ,  $j = 0.4$ 



Vertical oscillation,  $m = 0$ ,  $j = 0.4$ 

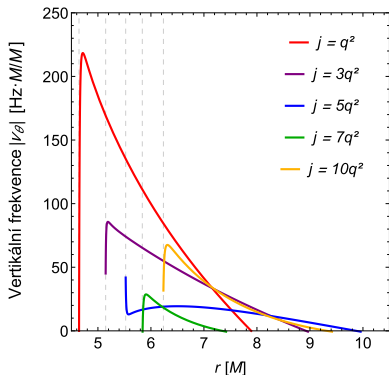
# Vertical oscillation, $m = -1, j = 0.4$



# Summary

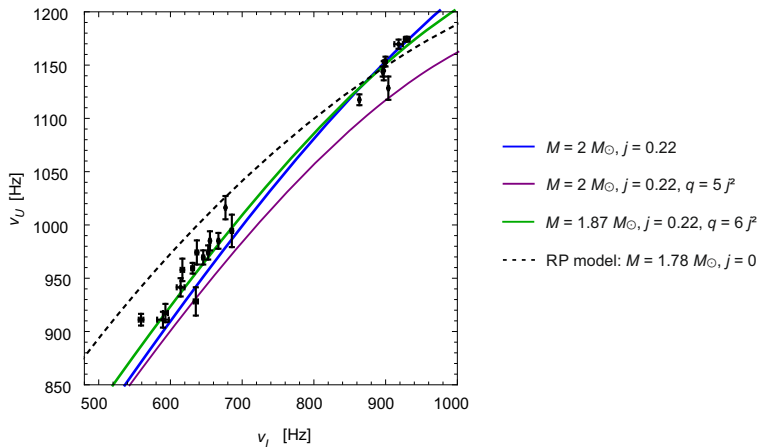
## Influence of quadrupole moment

- ▶ With increasing  $q$  decrease of maximum frequency values.
- ▶ Change of permissible torus position ( $r_{ms}$ ,  $r_{mb}$ ).
- ▶ Different behavior of the vertical non-axisymmetric mode ( $m = -1$ ).



# Modeling kHz QPO

Cusp model - Török et al. 2015 (source 4U 1636-53)



# References



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M. A. Abramowicz et al. “The Hartle-Thorne circular geodesics”. In: (Dec. 15, 2003). arXiv: gr-qc/0312070v1 [gr-qc].



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