

# Energetic Properties of Magnetized Neutron Stars in General Relativity

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**23 October 2020, RAGtime 22, Opava**



# PhD / postdoc under supervision of Zdenek



Habilitation DSc. thesis has been defended in 2016, more than 65 papers/WoS h-index  $> 22$ ; The Best Young Researcher 2017 WoS Award; The Best Researcher in Engineering 2019 Scopus Award

Habilitation DSc. defended in 2019/more than 35 papers/The best young scientist of JINR, Dubna 2015; Award of the Czech Ministry of Education for the best young researcher 2018; Award of the Czech Physical Society for the best young researcher 2020



PhD study at Silesian University in Opava, Czech Republic

PhD thesis is defended in 2018/more than 25 papers/ WoS h-index  $> 14$ ; Award of the Czech Physical Society for the best PhD thesis 2018; The Best Young Researcher 2019 Scopus







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## 2 Neutron Stars: Pulsars and Magnetars

## 3 Plasma magnetosphere of neutron stars in GR

Plasma MS of rotating and oscillating NSs in GR

GR magnetosphere of pulsar and Particle acceleration in a polar cap

Part time pulsars

Relativistic death line for magnetars

Death line for rotating and oscillating magnetars

Particle acceleration in NS magnetospheres

## 4 Subpulse drift velocity of pulsar magnetosphere within the space-charge limited flow model

Phenomena of drifting subpulses

Existing models for the drifting subpulses

Our results in frame of the space charge limited flow model

## 5 Conclusion









# GPS Stations by GFZ-Potsdam in Tashkent, Maidanak and Kitab



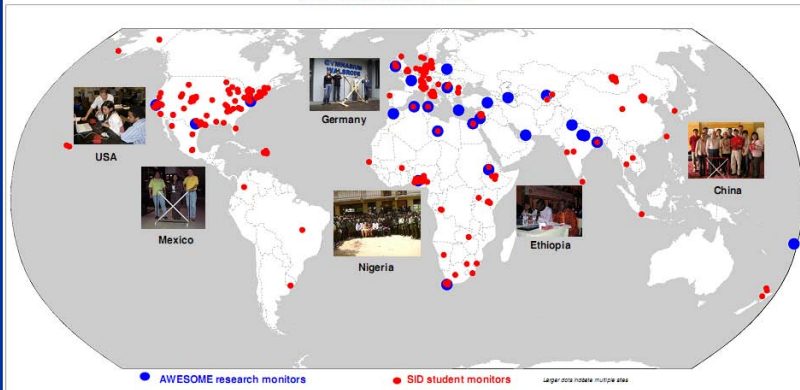
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| <br> | <br>                             | Umran Inan       | <b>Prof. Hans J. Haubold</b><br><i>UN Office for Outer<br/>Space Affairs<br/>Vienna International<br/>Centre</i> |
|  | <br> STANFORD<br>SOLAR<br>CENTER | Deborah Scherrer |  |

# World SID & AWESOME Sites



## Space Weather Monitor Sites

IHY Distribution 2007-2009



USA



Romania



Lebanon



Thailand







## Uzbekistan Intensifying the Work to Promote the Legacy of Mirzo Ulughbek, Astronomy and Aeronautics

Date Added: **15-09-2017**

Yesterday the President of Uzbekistan Shavkat Mirziyoyev signed the Resolution 'On the establishment of the Mirzo Ulughbek state specialized general boarding school and the Astronomy and Aeronautics Park.'

The boarding school with in-depth study of mathematics, astronomy, physics and informatics for 200 pupils and 150 places for students is created under the Astronomical Institute of the Academy of Sciences (the number of students in the future can be changed).

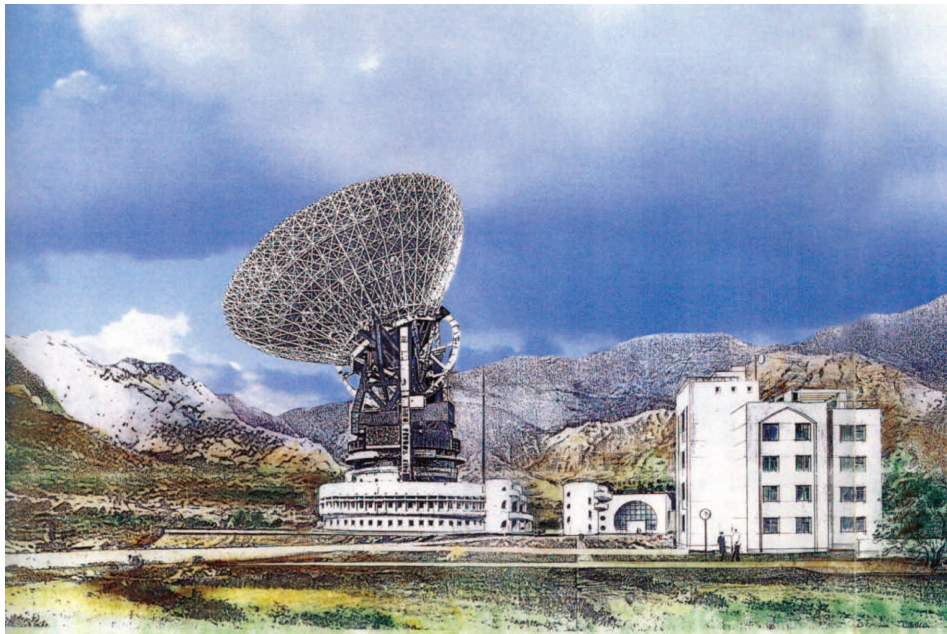
The Astronomical Institute has been instructed to ensure the participation of leading specialists in the school's educational process, in organizing lessons and practical exercises in astronomy using the available equipment.

The Astronomy and Aeronautics Park and the Planetarium as well as the boarding school will be located on the territory of the Astronomical Institute. Within the framework of the construction, it is planned to overhaul the main and historical buildings of the Institute, as well as pavilions of telescopes representing cultural and historical value.

The park will accommodate samples (models) of aircraft that are under the jurisdiction of the Ministry of Defense, the Uzbekistan Airways National Air Company and JSC Tashkent Mechanical Plant.

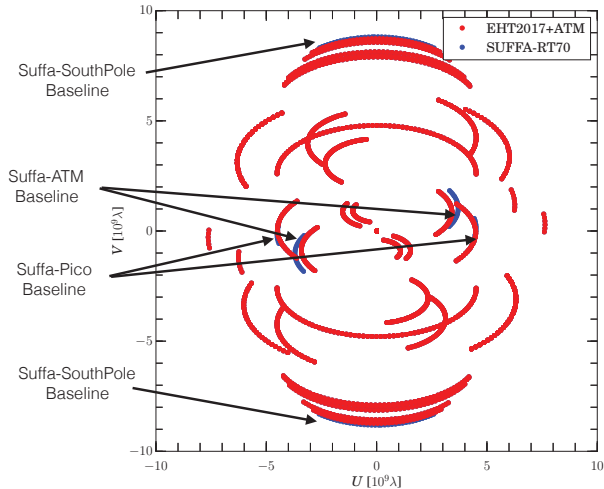




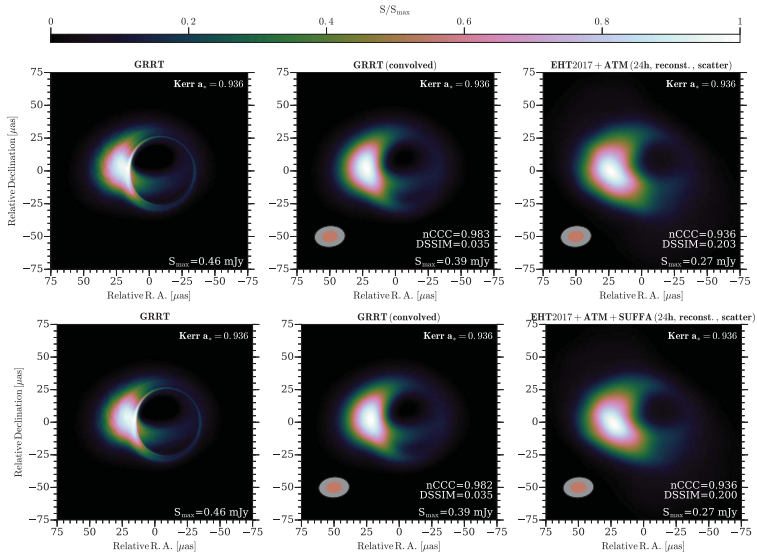


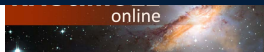
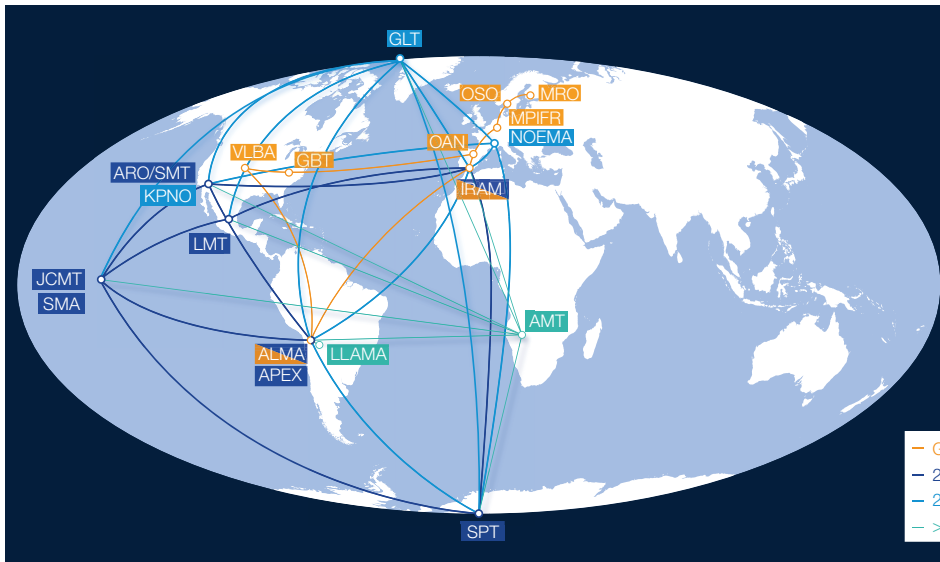
# Test case: Kerr $a=0.936$

using 24h of observations



# Test case: Kerr $a=0.936$





online

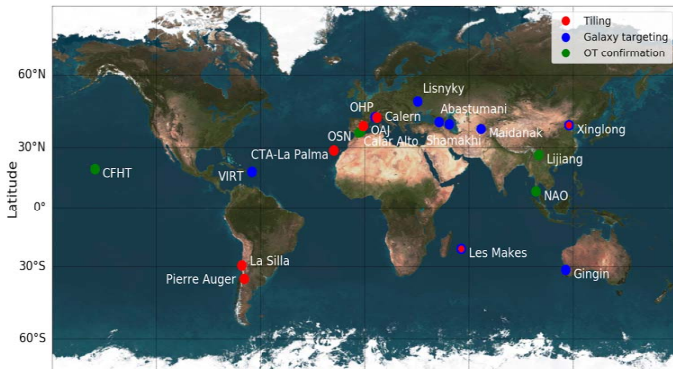




# GRANDMA - Global Rapid Advanced Network Devoted to multimessenger addicts

20 observatories - 29 institutes/groups

*PI. S. Antier (France)*



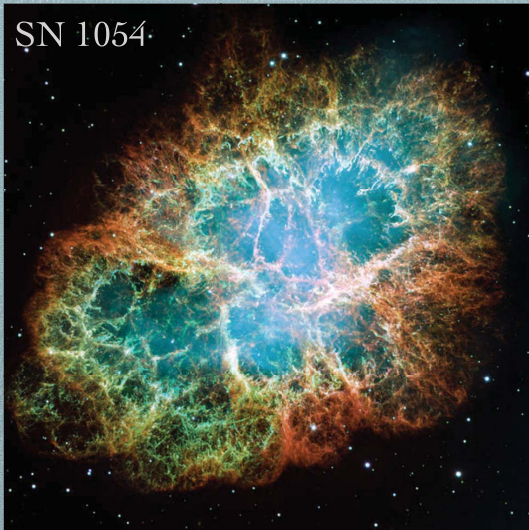
# Maidanak observatory

- Participates in GRANDMA with two 60 cm telescopes – Northern Zeiss-600 (NT) and Southern Zeiss-600 (ST)





## SN 1054



- \* Supernova explosions are spectacular events, marking the end of stellar life

- \* During maximum brightness, the supernova may briefly outshine an entire galaxy

- \* Before the development of the telescope, there have only been 5 supernovae seen in the last millennium

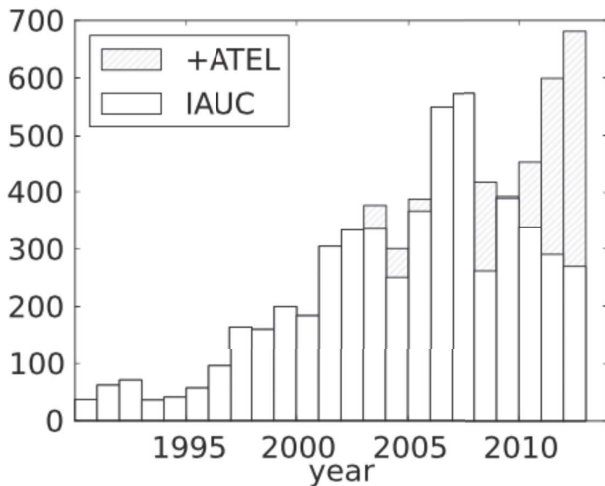
# SN 1006 – Ibn Sina Supernova Record in Arabic

نارا خالصة ، ولا يكون لها برد مطفى ، ولا أيضا تصعد صعودا سريرا ممعنا في حيز النار إلى أن تبلغ المكان الشديد قوة الدارية ، فيعرض لذلك أن يبقى التهابها واشتعالها مدة طويلة إما على صورة ذؤابة أو ذنب ، وأكثره شمالي وقد يكون جنوبيا ، وإما على صورة كوكب من الكواكب ، كالذى ظهر في سنة سبع وتسعين وثلاث مائة للهجرة ، فبقى قريبا من ثلاثة أشهر يلفظ ويلطف حتى اضمحل ، وكان في ابتدائه إلى السواد والخضرة ، ثم جعل كل وقت يرمى بالثمر ويزداد يابا ويلطف حتى اضمحل . وقد يكون على صورة لحية ، أو صورة حيوان له قرون ، وعلى سائر الصور ، وإنما يكون ذلك إذا كانت هناك مادة كثيفة واقنة ، تالفت أجزاءها يسيرا يسيرا وتحتل عنه متصعدة كروائد شمرية أو قرنية . ومنها المسماة أدترا كأن ثمريرها تسعير . وكل ما ثبت منها

- 
- (١) بالعدد : وبالعدد ، سا || فى : سافطة من ب ، ط (٢) كالوجود : كالوجود  
 د ، ط ، م (٣) ويحلقها غيرها : ويحلقه غيره ب ، د ، سا ، ط || موضعها : موضع ب ، د ، سا ، ط .  
 (٥) فى حقيقة : وحقيقة سا (٧) مقامه : مكانه د ، سا || يشتعل : سافطة من د .  
 (٨) وغفوة : غفوة سا (٩) وغلت : وحصلت سا . (١٠) وذات : ذات سا



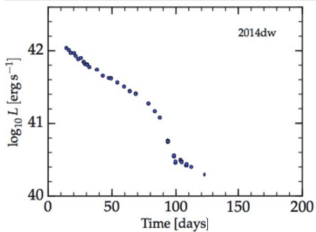
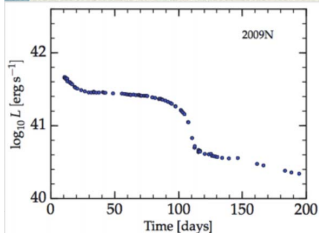
## Number of SN discoveries per year



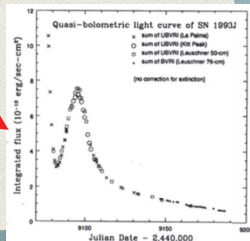
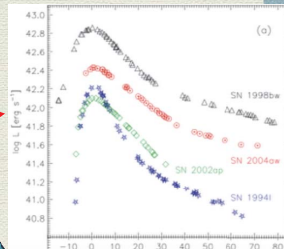
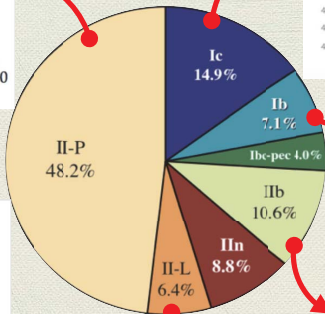
IAUC - International Astronomical Union Circulars

ATEL - The Astronomer's Telegram

# Different types of core-collapse SNe



Type II -> H lines  
Type I -> no H lines



# SN2017ein supernova

The supernova SN2017ein was discovered on 2017 May 25.99 (UT), in the nearby galaxy NGC 3938. It was observed on 25.77 (UT) at Maidanak observatory. Optical spectra obtained on May 26.6 (UT) indicated the supernova to be of Type Ic, about one week before maximum.



# Reconstructing quasi-bolometric lightcurve

Bolometric correction to B-band (*Lyman et al. 2014*)

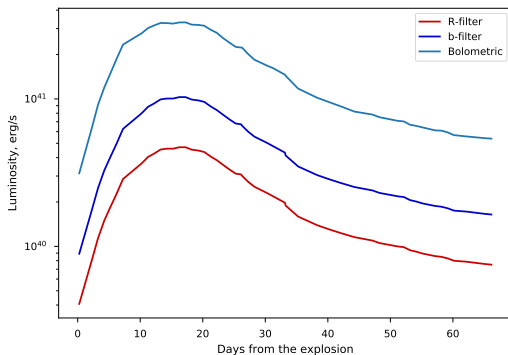
$$BC = -0.029 - 0.302 (B - R) - 0.22 (B - R)^2$$



# Reconstructing quasi-bolometric lightcurve

Bolometric correction to B-band (*Lyman et al. 2014*)

$$BC = -0.029 - 0.302 (B - R) - 0.22 (B - R)^2$$



# Fitting to the model

## The model

- Photospheric phase,  $t \leq 30$  days - *Arnett (1992)*
- Nebular phase,  $t \geq 60$  days - *Sutherland, Wheeler (1984)*

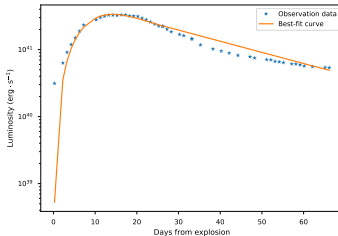




# Fitting to the model

## The model

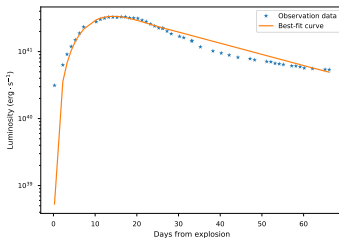
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# Fitting to the model

## The model

- Photospheric phase,  $t \leq 30$  days - *Arnett (1992)*
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$$M_{Ni} = 0.037M_{\odot}, \quad M_{ej} = 1.246M_{\odot}, \quad E_k = 1.641 \cdot 10^{51} \text{ erg}$$

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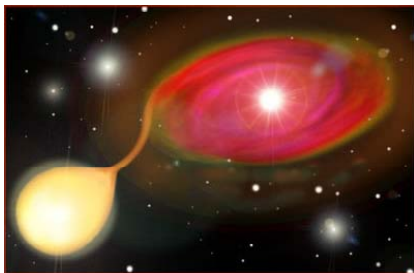
## 5 Conclusion



# Classical neutron stars

In 60s the first X-ray sources have been discovered.

They were neutron stars in close binary systems, BUT ...  
.... they were «not recognized»....



Now we know hundreds of X-ray binaries with neutron stars in the Milky Way and in other galaxies.

## Accretion in close binaries

Accretion is the most powerful source of energy realized in Nature, which can give a huge energy output.

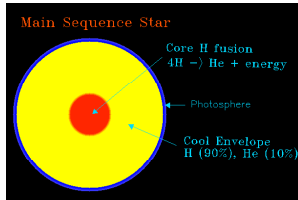
When matter fall down onto the surface of a neutron star up to 10% of  $mc^2$  can be released.



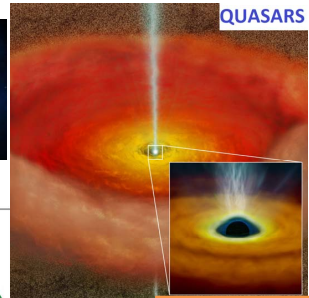
**RAGtime 22**

Zel'dovich *Sov. Phys. Dokl.* 9 195 (1964); Salpeter *Astrophys. J.* 140 796 (1964); Shakura & Sunyaev *Astron. Astrophys.* 24 337 (1973)

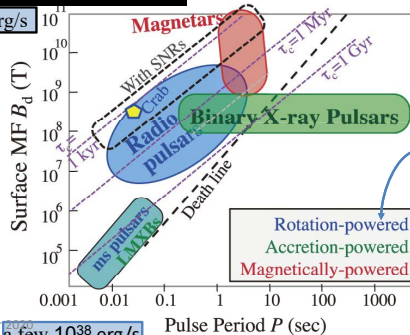
# ENERGETICS



a few  $10^{33}$  erg/s



a few  $10^{45}$  erg/s



21 October 2020

a few  $10^{38}$  erg/s

T.Gold, Nature, 1968

Moreover, oscillating-powered pulsars/magnetars model has also been suggested and shown how oscillating kinetic energy transforms to EM radiation energy.

4

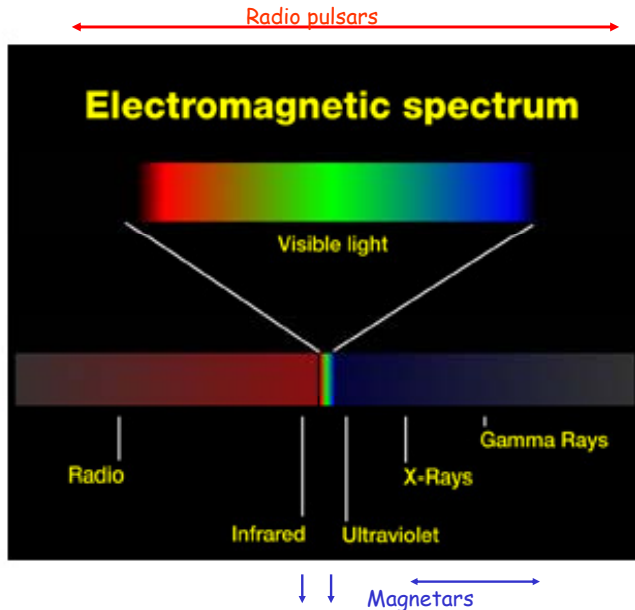
## NSs

- RADIO PULSARS: 2000 discovered to date
- Radiate covering most of the electromagnetic spectrum
- Rotate with periods that span five decades (ms to a few hours)
- Are **powered** by their own rotational energy, residual surface heat or accretion
- Live tens of millions of years

29 magnetars: 15 SGRs (11 confirmed, 4 candidates), and 14 AXPs (12 confirmed, 2 candidate) discovered to date:

<http://www.physics.mcgill.ca/pulsar/magnetar/main.html>

- Magnetars are magnetically powered, rotating neutron stars
- Radiate almost entirely in X-rays, with luminosities  $10^{33}$  to  $10^{36}$  erg/s
- Emit typically brief (1-100 ms) bursts and very rarely, Giant Flares
- Rotate in a very narrow period interval (2-11 s) and slow down faster than any other object ( $10^{-10}$ - $10^{-11}$  s/s $^{-1}$ )
- **Powered** by MF energy, which heats the NS and the surface glows persistently in X-rays, and fractures the crust inducing short, repeated bursts
- Die rather young; typical ages are 10 000 yrs

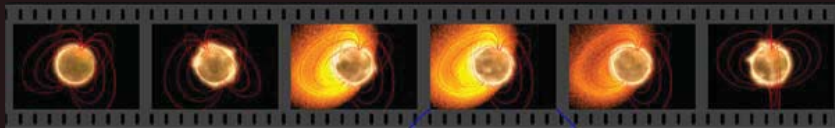




# Magnetars

- $dE/dt > dE_{\text{rot}}/dt$
- By definition: The energy of the magnetic field is released

Magnetic fields  $10^{14}$ – $10^{15}$  G



# Gravitational collapse of the magnetized star

Due to conservation of magnetic flux during collapse

$$BR^2 = \text{const} \Rightarrow B = B_0 (R_0/R)^2$$

in the nonrelativistic limit magnetic moment  $\mu \sim BR^3$  decays as

$$\mu = \mu_0 (R/R_0) \Rightarrow \lim_{R \rightarrow 0} \mu = 0 .$$

In GR during collapse magnetic moment decays as

$$\mu(t) = \mu_0 (4M^2/3R_0 ct) ,$$

and exterior magnetic field should decay with  $t^{-1}$  (Ginzburg & Ozernoy 1964, Anderson & Cohen 1970, Zeldovich & Novikov 1971).

The correct decay rate at late times of an initially static dipole electromagnetic radiation field outside a black hole is  $t^{-(2l+2)}$  (Price 1972, Thorne 1971).

# NS Magnetosphere

EF on the Star Surface:

$$E \propto \frac{\Omega R}{c} B \propto \frac{\Omega \xi}{c} B \propto 10^{10} \text{V} \cdot \text{cm}^{-1}$$

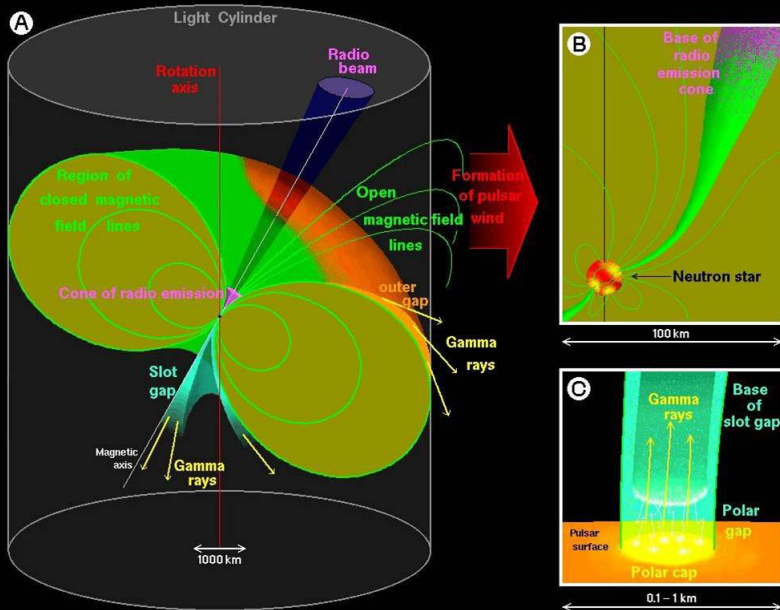
Goldreich & Julian, 1969, *Astrophys.J.*, 157, 869

Cascade generation of electron-positron plasma leads to formation of MS with plasma screening longitudinal EF.

Plasma is corotating with the neutron star.

Charges along open field lines create plasma modes.





## Oscillating NSs

- NSs are endowed with intense EM fields, but they are also subject to oscillations of various type.
- Evidence for stellar oscillations coming from the observation of QPOs following giant flares of SGRs (Israel et al., 2005; Strohmayer & Watts, 2005; Watts & Strohmayer, 2006, 2007).
- The study of internal structure of NSs is of great importance for fundamental physics because matter inside NS is under extreme conditions. The study of proper oscillations of isolated NSs may provide an opportunity to obtain important information about the internal structure of these objects.

# Model Assumptions

Difficulty of simultaneously solving the Maxwell eqs

$$3!F_{[\alpha\beta,\gamma]} = 2(F_{\alpha\beta,\gamma} + F_{\gamma\alpha,\beta} + F_{\beta\gamma,\alpha}) = 0, \quad F^{\alpha\beta}_{;\beta} = 4\pi J^\alpha,$$

and the highly nonlinear Einstein eqs

$$R_{\alpha\beta} - \frac{1}{2}g_{\alpha\beta}R = \kappa T_{\alpha\beta}, \quad T_{\alpha\beta} = T_{(G)\alpha\beta} + T_{(em)\alpha\beta}.$$

E/M Fields are considered in a given background Geometry: Very Good Approximation

$$T_{(G)\alpha\beta} \gg T_{(em)\alpha\beta}, \quad T_{\alpha\beta} \approx T_{(G)\alpha\beta}.$$



# Model Assumptions

MF does not contribute to the total energy momentum

$$\frac{B^2}{8\pi\langle\rho_0\rangle c^2} \simeq 1.6 \times 10^{-6} \left( \frac{B}{10^{15} \text{ G}} \right)^2 \left( \frac{1.4 M_\odot}{M} \right) \left( \frac{R}{15 \text{ Km}} \right)^3 .$$

Space-time metric

$$ds^2 = -e^{2\Phi(r)} dt^2 + e^{2\Lambda(r)} dr^2 - 2\omega(r)r^2 \sin^2 \theta dt d\phi + r^2 d\theta^2 + r^2 \sin^2 \theta d\phi^2 .$$

$\omega(r)$  is the Lense-Thirring angular velocity and outside the star is given by

$$\omega(r) \equiv \frac{d\phi}{dt} = -\frac{g_{0\phi}}{g_{\phi\phi}} = \frac{2J}{r^3} .$$

$N \equiv (1 - 2M/r)^{1/2}$  is lapse function,  $\omega_{\text{LT}} = 2aM/r^3$  is the Lense-Thirring angular velocity,  $R$  is the star radius,  $\eta = r/R$  is the dimensionless radial coordinate,  $\varepsilon = 2M/R$  is the compactness parameter,  $\beta = I/I_0$  is the moment of inertia of the star in units of  $I_0 = MR^2$  and  $\kappa = \varepsilon\beta$ .

# Model Assumptions

## Velocity perturbation

$$\delta u^\alpha = \Gamma \left( 1, \delta v^i \right) = \Gamma \left( 1, e^{-\Lambda} \delta v^{\hat{r}}, \frac{\delta v^{\hat{\theta}}}{r}, \frac{\delta v^{\hat{\phi}}}{r \sin \theta} \right) .$$

For small velocity perturbations  $\delta v^i/c \ll 1$ :

$$\Gamma = \left[ -g_{00} \left( 1 + g_{ik} \frac{\delta v^i \delta v^k}{g_{00}} \right) \right]^{-1/2} \simeq e^{-\Phi} .$$

## Toroidal Oscillations

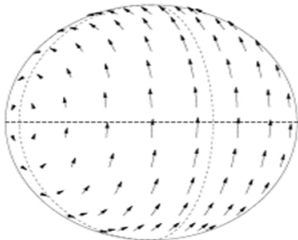
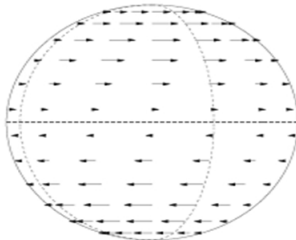
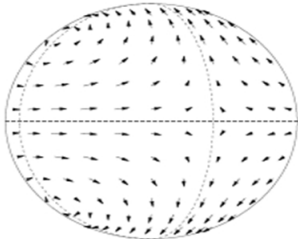
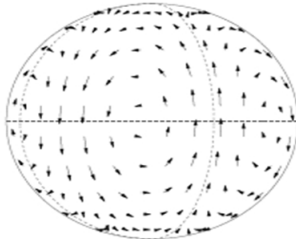
$$\delta v^{\hat{i}} = \left\{ 0, \frac{1}{\sin \theta} \partial_\phi Y_{\ell' m'}(\theta, \phi), -\partial_\theta Y_{\ell' m'}(\theta, \phi) \right\} \eta(r) e^{-i\omega t} .$$

Frequency range for small velocity perturbations

$$\omega \bar{\xi} \ll c, \quad \bar{\xi} \approx 10^{-3} R = 10^3 \text{ cm}, \quad \omega \ll 3 \times 10^7 \text{ Hz} .$$



# Toroidal Oscillations

 $l=1, m=1$ 

 $l=2, m=0$ 

 $l=2, m=1$ 

 $l=3, m=3$ 


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# GR Effects in Pulsar MS

## Goldreich-Julian charge density

$$\rho_{GJ} = -\frac{\Omega B_0}{2\pi c} \frac{1}{N\eta^3} \frac{f(\eta)}{f(1)} \left\{ 1 - \frac{\kappa}{\eta^3} - L \left( 1 - \frac{\varepsilon}{\eta} \right) \frac{1}{\eta^2} \frac{4 \sin^2 \frac{\theta}{2}}{\sin^2 \theta} \right\} .$$

Charge density  $\rho$  is proportional to MF with the proportionality coefficient being constant along the given MF line

$$\rho = \frac{\Omega B_0}{2\pi c} \frac{1}{N\eta^3} \frac{f(\eta)}{f(1)} A(\xi) ,$$

where  $\xi = \theta/\Theta$ , and polar angle  $\Theta$  of the last open magnetic line

$$\Theta \cong \sin^{-1} \left\{ \left[ \eta \frac{f(1)}{f(\eta)} \right]^{1/2} \sin \Theta_0 \right\} , \quad \Theta_0 = \sin^{-1} \left( \frac{R}{R_{LC} f(1)} \right)^{1/2} ,$$

**RAGtime 22**

Muslimov & Tsygan (1990, 1992), Beskin (1990), Muslimov & Harding (1997)

# GR Effects in Pulsar MS

EF  $E_{\parallel}$  is

$$E_{\parallel} = -E_{vac} \Theta_0^2 \frac{3(\kappa - L\varepsilon)}{2\eta^4} (1 - \xi^2) ,$$

where  $E_{vac} \equiv (\Omega R/c) B_0$ .

The ratio of polar-cap energy losses

$$\frac{(L_p)_{max}}{(L_p)_{max} (l=0)} = 1 - \frac{L(\kappa + \varepsilon - 2\kappa\varepsilon)}{\kappa(1 - \kappa)} + \frac{L^2\varepsilon(1 - \varepsilon)}{\kappa(1 - \kappa)} .$$

V. S. Morozova, B. J. Ahmedov and V. G. Kagramanova, General Relativistic Effect of Gravitomagnetic Charge on Pulsar Magnetosphere and Particle Acceleration in a Polar Cap, **ApJ**, 2008, V 684, 1359.



# GJ charge density for slowly rotating and oscillating NS

$$\rho_{\text{GJ}} = -\frac{\Omega B_0}{2\pi c} \frac{1}{\alpha \bar{r}^3} \frac{f(\bar{r})}{f(1)} \left(1 - \frac{\kappa}{\bar{r}^3}\right) - \frac{1}{4\pi c} \frac{1}{R \bar{r}^4} \frac{B_0 e^{-i\omega t}}{\Theta^2(\bar{r})} \frac{1}{N} \frac{f(\bar{r})}{f(1)} \tilde{\eta}(\bar{r}) l'(l' + 1) Y_{l'm'}.$$

Using small angles  $\theta$  approximation

$$Y_{l'm'}(\theta, \phi) \approx A_{l'm'}(\phi) \theta^m,$$

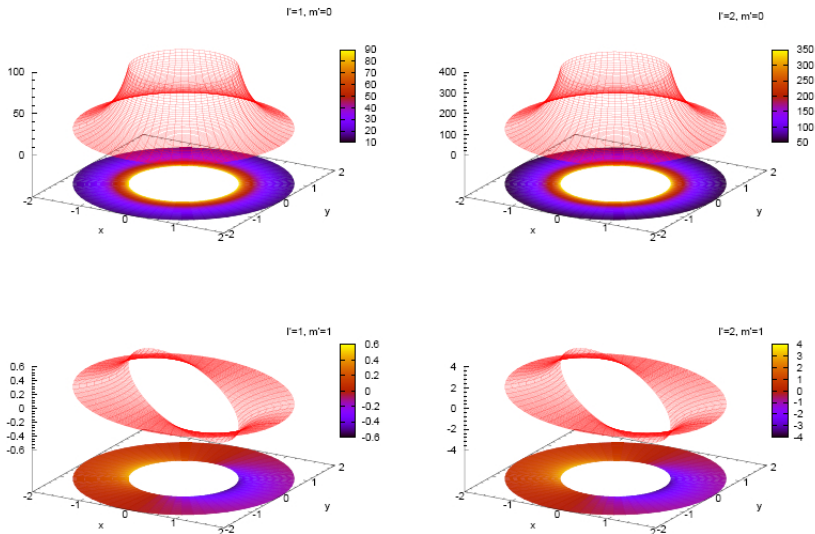
one could get the ratio  $\delta\rho_{\text{GJ } l'm'}/\rho_{\text{GJ},0}$  in the form

$$\delta\rho_{\text{GJ } l'm'}/\rho_{\text{GJ},0} = \frac{K}{2\bar{r}^{2-m/2}} \Theta_0^{m-2} \left( \frac{f(\bar{r})}{f(1)} \right)^{\frac{2-m}{2}} \frac{l'(l' + 1) A_{l'm'}(\phi)}{\left(1 - \frac{\kappa}{\bar{r}^3}\right)},$$

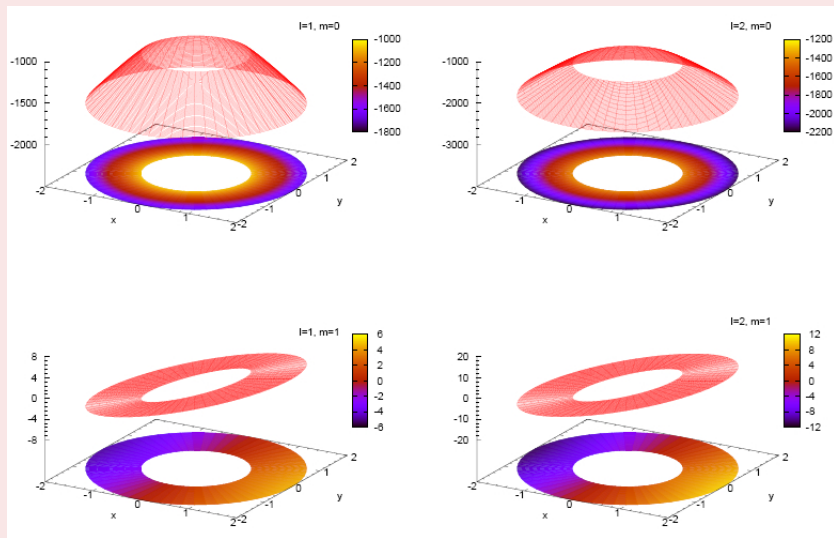
where  $K = \tilde{\eta}(1)/\Omega R$ .



Ratio  $\delta\rho_{\text{GJ}}/\rho_{\text{GJ},0}$  for the mode (1, 0) (left-hand top panel), (1, 1) (left-hand bottom panel), (2, 0) (right-hand top panel) and (2, 1) (right-hand bottom panel). NS parameters  $\kappa = 0.15$ ,  $\varepsilon = 1/3$ ,  $K = 0.01$ ,  $\Theta_0 = 0.008$ ,  $\Omega = 1 \text{ rad s}^{-1}$ .



Ratio of longitudinal component of EF to  $E_0$  for the mode (1, 0) (left-hand top panel), (1, 1) (left-hand top panel), (2, 0) (right-hand top panel) and (2, 1) (right-hand bottom panel).





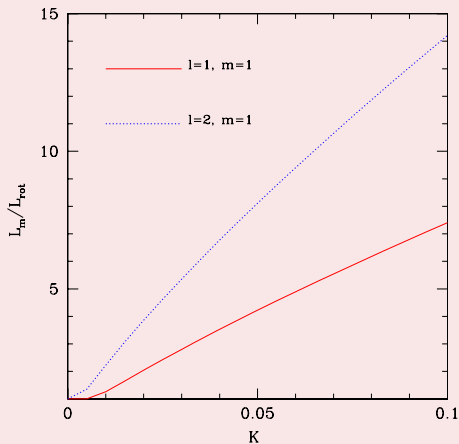
## Energy losses of slowly rotating and oscillating NS

$$\begin{aligned}
 L_{|m \neq 0} = & R^3 N_R B_0^2 \left| \left\{ \frac{\Omega^2 R}{2c N_R} (1 - \kappa)^2 \frac{\Theta_0^4}{4} \right. \right. \\
 & + \frac{\Omega}{4c} \frac{1}{N_R} (1 - \kappa) \tilde{\eta}(1) l(l+1) A_{lm} \frac{\Theta_0^{m+4}}{m+4} \\
 & - \frac{\Omega}{2c} \frac{1}{N_R} (1 - \kappa) A_{lm} \tilde{\eta}(1) \frac{\Theta_0^{m+2}}{m+2} \\
 & \left. \left. - \frac{1}{2c} \frac{1}{R N_R} A_{lm}^2 \tilde{\eta}^2(1) l(l+1) \frac{\Theta_0^{2m+2}}{2m+2} \right\} \right|
 \end{aligned}$$

and

$$\begin{aligned}
 L_{|m=0} = & R^3 N_R B_0^2 \frac{\Theta_0^4}{8} \left| [\Omega R (1 - \kappa) - A_{l0} \tilde{\eta}(1)] \left\{ \frac{\Omega}{c N_R} (1 - \kappa) \right. \right. \\
 & \left. \left. + \frac{1}{2c} \frac{1}{N_R} \tilde{\eta}(1) l(l+1) A_{l0} \right\} \right|.
 \end{aligned}$$

The ratio  $L_m/L_{rot}$  as a function of parameter  $K = \tilde{\eta}(1)/\Omega R$  for modes (1, 1) (continuous red line) and (2, 1) (dotted blue line).



# Constrains on parameters of Einstein-Aether gravity

## Radio-load isolated NSs

P. A. Caraveo, Annual Review of Astronomy and Astrophysics, (2014)

| Neutron star      | Period, P<br>millisecond | $\frac{dP}{dt} \times 10^{-15} \text{ s/s}$ | $c_{13}, (c_{14}=0)$<br>ICS | $c_{14}, (c_{13}=0)$<br>ICS | $c_{13}, (c_{14}=0)$<br>CR | $c_{14}, (c_{13}=0)$<br>CR |
|-------------------|--------------------------|---|-----------------------------|-----------------------------|----------------------------|----------------------------|
| PSR J1057 – 52269 | 197.114                  | 5.83  | 0.952158                    | -39.8041                    | 0.98342                    | -42.3326                   |
| PSR J1509 – 5850  | 88.925                   | 9.17  | 0.951734                    | -39.4366                    | 0.98658                    | -41.6524                   |
| PSR J1952 + 3252  | 39.534                   | 5.83  | 0.951968                    | -39.9528                    | 0.98698                    | -42.1368                   |
| PSR J2030 + 3641  | 200.129                  | 6.51  | 0.952169                    | -39.8139                    | 0.97986                    | -43.0021                   |
| PSR J2043 + 2740  | 96.131                   | 1.23  | 0.952085                    | -39.7405                    | 0.97963                    | -43.0124                   |

## Radio-quiet isolated NSs

S.Mereghetti, Astrophysics and Space Science 2011

| Neutron star     | Period, P<br>millisecond | $\frac{dP}{dt} \times 10^{-15}$ s/s | $c_{13}, (c_{14}=0)$<br>ICS | $c_{14}, (c_{13}=0)$<br>ICS | $c_{13}, (c_{14}=0)$<br>CR | $c_{14}, (c_{13}=0)$<br>CR |
|------------------|--------------------------|-------------------------------------|-----------------------------|-----------------------------|----------------------------|----------------------------|
| PSR J1746 – 3239 | 199.541                  | 6.56                                | 0.952171                    | -39.8153                    | 0.98465                    | -42.6547                   |
| PSR J0106 + 4855 | 83.157                   | 0.428                               | 0.951896                    | -39.3827                    | 0.98015                    | -43.0154                   |
| PSR J1836 + 5925 | 173.264                  | 1.5                                 | 0.951938                    | -39.3482                    | 0.98652                    | -43.65812                  |
| PSR J2028 + 3332 | 176.707                  | 4.86                                | 0.952156                    | -39.8026                    | 0.9845                     | -42.6895                   |
| PSR J2139 + 4716 | 282.849                  | 1.8                                 | 0.951767                    | -39.4654                    | 0.98432                    | -43.0098                   |
| PSR J2030 + 4415 | 227.070                  | 6.49                                | 0.952144                    | -39.7917                    | 0.98654                    | -42.3651                   |
| PSR J1957 + 5033 | 374.806                  | 6.83                                | 0.952022                    | -39.6858                    | 0.97986                    | -42.3651                   |
| PSR J2055 + 2539 | 319.561                  | 4.11                                | 0.95196                     | -39.6324                    | 0.9814                     | -41.9856                   |

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Phenomena of drifting subpulses

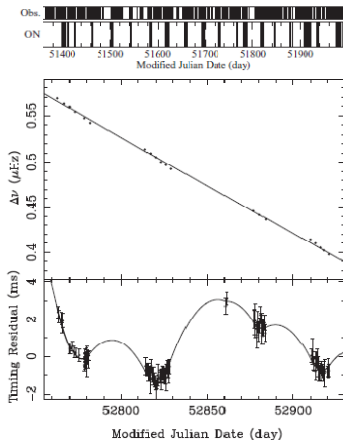
Existing models for the drifting subpulses

Our results in frame of the space charge limited flow model

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## Part time (Intermittent) pulsars (PSR 1931+24)



21 October 2020

Kramer et.al, Nature, 2006

- Only visible for 20 % of time
- ON period 5-10 days
- OFF period 25-35 days
- Spin period 813ms
- Distance 4,6 kpc

$$\dot{\nu}_{ON} = -16.3 \times 10^{-15} \text{ Hz/s}$$

$$\dot{\nu}_{OFF} = -10.8 \times 10^{-15} \text{ Hz/s}$$

Bing Zhang et.al MNRAS 2006

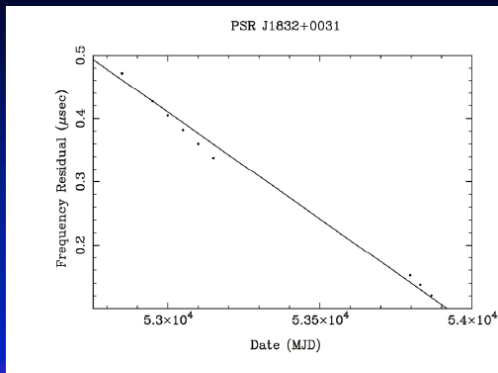
REACTIVATED DEAD PULSAR

8

## More intermittent pulsars

## Properties: J1832+0031

- 'on' state >300 days
- 'off' state ~700 days
- Quasi-periodicity ?
- Increase in slow-down rate during 'on' state similar to B1931+24



## Possible explanations

- **Nulling?** (Backer (1970))

*Nulling phenomenon lasts only for a few pulse periods and not on a time-scales of tens of days*

- **Precession?**

*Cannot produce a transition from the ON to the OFF state in less than 10 s*

- **Global failure of charge particles currents in the magnetosphere?** (Lyne (2009), Gurevich&Istomin (2007))

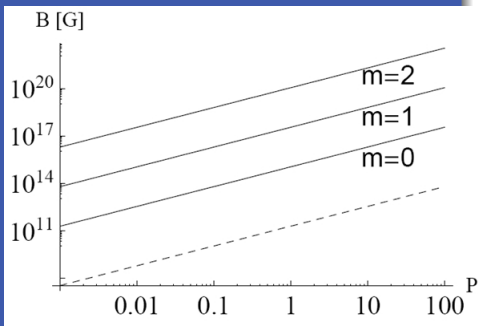
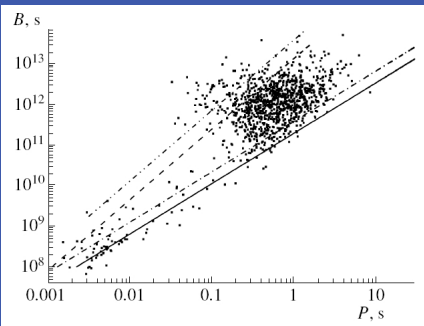
*Lack of a physical mechanism for changing the plasma flow in the magnetosphere in such a drastic way*

There is no self-consistent explanation of the phenomena yet



Transition from the OFF to the ON state of intermittent pulsar could correspond to the reactivation of a 'dead' pulsar above 'death line' (Zhang, Gil & Dyks, 2007)

Death line is the  $P - \dot{P}$  or  $P - B$  diagram which indicates the region where pulsar can support radio emission from magnetosphere (Kantor, Tsygan, 2004).



Ahmedov B.J., Morozova V.S. Plasma Magnetosphere Formation Around Oscillating Magnetized Neutron Stars, **ApSS**, 2009, V. 319, 115

## Damping times of toroidal modes for a neutron star

| Mode   | $\nu$ (kHz)<br>(1) | $E_T$ (erg)<br>(2)    | $L_{em}^{Newt}$ (erg s $^{-1}$ )<br>(3) | $L_{em}^{GR}$ (erg s $^{-1}$ )<br>(4) | $\tau_{gw}$ (s)<br>(5) | $\tau_{em}^{Newt}$ (s)<br>(6) | $\tau_{em}^{GR}$ (s)<br>(7) | $\tau_{gw}/\tau_{em}^{GR}$<br>(8) | $\tau_{em}^{Newt}/\tau_{em}^{GR}$<br>(9) |
|--------|--------------------|-----------------------|---|---------------------------------------|------------------------|-------------------------------|-----------------------------|-----------------------------------|--|
| $1t_1$ | 17.9               | $1.09 \times 10^{49}$ | $1.77 \times 10^{43}$                   | $1.57 \times 10^{44}$                 | ...                    | $1.23 \times 10^6$            | $1.39 \times 10^5$          | ...                               | 8.85                                     |
| $1t_2$ | 30                 | $6.40 \times 10^{48}$ | $1.44 \times 10^{44}$                   | $1.28 \times 10^{45}$                 | ...                    | $8.88 \times 10^4$            | $1.00 \times 10^4$          | ...                               | 8.88                                     |
| $1t_3$ | 43                 | $1.59 \times 10^{48}$ | $5.98 \times 10^{44}$                   | $5.30 \times 10^{45}$                 | ...                    | $5.32 \times 10^3$            | $6.00 \times 10^2$          | ...                               | 8.87                                     |
| $1t_4$ | 52.7               | $2.72 \times 10^{47}$ | $1.33 \times 10^{45}$                   | $1.18 \times 10^{46}$                 | ...                    | $4.08 \times 10^2$            | $4.60 \times 10^1$          | ...                               | 8.87                                     |
| $2t_0$ | 0.36               | $3.31 \times 10^{47}$ | $6.86 \times 10^{32}$                   | $3.45 \times 10^{33}$                 | $6.62 \times 10^{11}$  | $9.65 \times 10^{14}$         | $1.92 \times 10^{14}$       | $3.45 \times 10^{-3}$             | 5.03                                     |
| $2t_1$ | 17.9               | $3.26 \times 10^{49}$ | $9.32 \times 10^{42}$                   | $4.96 \times 10^{43}$                 | $7.60 \times 10^5$     | $7.00 \times 10^6$            | $1.31 \times 10^6$          | 0.58                              | 5.34                                     |
| $2t_2$ | 30                 | $1.92 \times 10^{49}$ | $2.17 \times 10^{44}$                   | $1.15 \times 10^{45}$                 | $2.33 \times 10^5$     | $1.77 \times 10^5$            | $3.33 \times 10^4$          | 70                                | 5.32                                     |
| $2t_3$ | 43                 | $4.76 \times 10^{48}$ | $1.83 \times 10^{45}$                   | $9.72 \times 10^{45}$                 | $1.51 \times 10^4$     | $5.21 \times 10^3$            | $9.79 \times 10^2$          | 15.43                             | 5.32                                     |
| $2t_4$ | 52                 | $8.15 \times 10^{47}$ | $6.10 \times 10^{45}$                   | $3.24 \times 10^{46}$                 | $4.68 \times 10^3$     | $2.67 \times 10^2$            | $5.03 \times 10^1$          | 93.04                             | 5.31                                     |

## Damping times of spheroidal modes for a neutron star

| Mode     | $\nu$ (kHz)<br>(1) | $E_T$ (erg)<br>(2)    | $L_{em}^{Newt}$ (erg s $^{-1}$ )<br>(3) | $L_{em}^{GR}$ (erg s $^{-1}$ )<br>(4) | $\tau_{gw}$ (s)<br>(5) | $\tau_{em}^{Newt}$ (s)<br>(6) | $\tau_{em}^{GR}$ (s)<br>(7) | $\tau_{gw}(s)/\tau_{em}^{GR}(s)$<br>(8) | $\tau_{em}^{Newt}/\tau_{em}^{GR}$<br>(9) |
|----------|--------------------|-----------------------|---|---------------------------------------|------------------------|-------------------------------|-----------------------------|---|--|
| $2p_2$   | 104.72             | $1.55 \times 10^{50}$ | $9.04 \times 10^{44}$                   | $4.56 \times 10^{45}$                 | $0.23 \times 10^{-3}$  | $3.43 \times 10^5$            | $6.79 \times 10^4$          | $0.34 \times 10^{-6}$                   | 4.4                                      |
| $2f$     | 28.56              | $1.59 \times 10^{52}$ | $2.38 \times 10^{43}$                   | $7.41 \times 10^{44}$                 | $7.50 \times 10^{-3}$  | $1.34 \times 10^9$            | $4.29 \times 10^7$          | $1.75 \times 10^{-10}$                  | 31.24                                    |
| $2s_2$   | 14.61              | $2.53 \times 10^{53}$ | $4.46 \times 10^{43}$                   | $1.03 \times 10^{45}$                 | $1 \times 10^4$        | $1.13 \times 10^{10}$         | $4.90 \times 10^8$          | $0.2 \times 10^{-4}$                    | 23.06                                    |
| $2s_1$   | 8.6                | $1.32 \times 10^{54}$ | $5.13 \times 10^{43}$                   | $1.12 \times 10^{45}$                 | $4.32 \times 10^4$     | $5.15 \times 10^{10}$         | $2.36 \times 10^9$          | $1.83 \times 10^{-5}$                   | 21.82                                    |
| $2i_2$   | 0.63               | $4.08 \times 10^{47}$ | $5.49 \times 10^{43}$                   | $1.16 \times 10^{45}$                 | $5.04 \times 10^9$     | $1.48 \times 10^4$            | $7.01 \times 10^2$          | $0.72 \times 10^7$                      | 21.11                                    |
| $2i_1$   | 0.35               | $1.63 \times 10^{53}$ | $5.49 \times 10^{43}$                   | $1.16 \times 10^{45}$                 | $8.64 \times 10^5$     | $5.93 \times 10^9$            | $2.80 \times 10^8$          | $3.1 \times 10^{-3}$                    | 21.18                                    |
| $2g_2^s$ | 0.12               | $5.49 \times 10^{43}$ | $5.49 \times 10^{43}$                   | $1.16 \times 10^{45}$                 | $7.57 \times 10^{16}$  | $5.24 \times 10^{-3}$         | $2.47 \times 10^{-4}$       | $3.1 \times 10^{20}$                    | 21.21                                    |
| $2g_3^s$ | 0.1                | $1.96 \times 10^{40}$ | $5.49 \times 10^{43}$                   | $1.16 \times 10^{45}$                 | $1.17 \times 10^{17}$  | $0.71 \times 10^{-3}$         | $0.34 \times 10^{-4}$       | $3.4 \times 10^{21}$                    | 20.88                                    |

## Alternative idea for the explanation of part time pulsars phenomena

- During the ON state pulsar is oscillating: stellar oscillations create relativistic wind of charged particles by virtue of additional accelerating electric field
- In a period of about 10 days the stellar oscillations are damped and the OFF period starts
- Quasi-periodic stellar glitches excite oscillations again, thus, being responsible for the emergence of new ON states with a certain periodicity

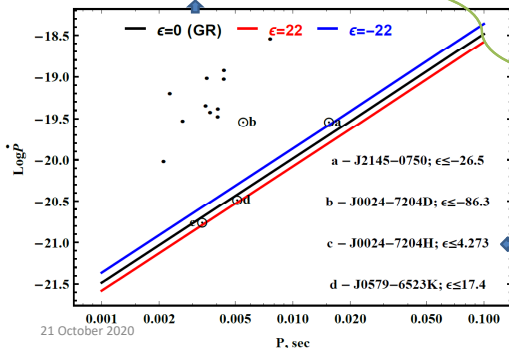


# Scheme for part-time pulsar model

Deathline for radio pulsars shifts up due to negative deformation, and limited by lower limit for the deformation parameter.

Schematic view for to explain the nature of part-time pulsars by time dependence of their deformation

$$L(t) = f(\epsilon(t)) \rightarrow \epsilon(t) = f^*(L(t))$$



from observational data for ON and OFF states

Fitting function for deformation parameter taking account the lower limit.

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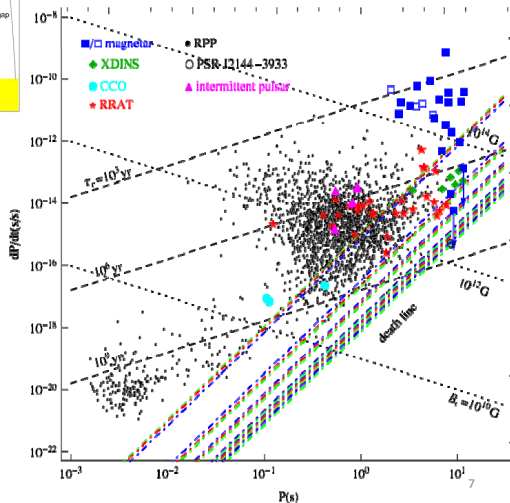
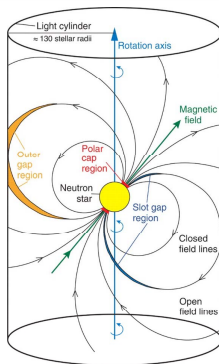
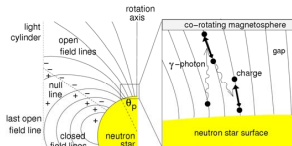
Our results in frame of the space charge limited flow model

## 5 Conclusion



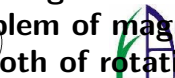
# Plasma magnetosphere of NS

Goldreich &amp; Julian 1969



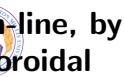
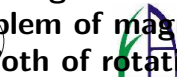
# Relativistic death line for magnetars

- The activity of magnetars is observed in the form of bursts in X-ray and  $\gamma$ -ray bands, while there is no periodic radio emission from the majority of magnetars in the same range of frequencies of ordinary pulsars.
- The absence of radio emission from magnetars is related to their slow rotation, i.e. the low energy of the primary particles, accelerated near the surface of the star.
- The death-line for magnetars, i.e. the line in the  $P - \dot{P}$  diagram that separates the regions where the neutron star may be radio-loud or radio-quiet.
- We consider the influence of magnetar oscillations on the conditions for the radio emission generation in the MS of magnetars and revisit the problem of magnetars death-line, by taking into account the role both of rotation and of toroidal oscillations in a relativistic framework.



# Relativistic death line for magnetars

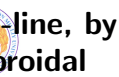
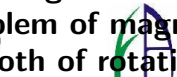
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The critical magnetic field is defined as  $B_c = m^2 c^3 / e \hbar \approx 4.414 \times 10^{13} \text{G}$ , where  $m$  is the electron mass and  $e$  is the electron charge.

When distance between two neighboring Landau levels becomes equal to the rest energy of the electron  $\hbar \omega_c = mc^2$ ,  $\omega_c = eB_c / mc$ .

Characteristic energy of the curvature gamma quanta is  $\epsilon_\gamma \approx \hbar c \gamma^3 / R_c$ .



# Dependence of death-lines from parameter $\kappa$

When  $\chi = 0$  the value of the magnetic field for which the generation of secondary plasma still possible is

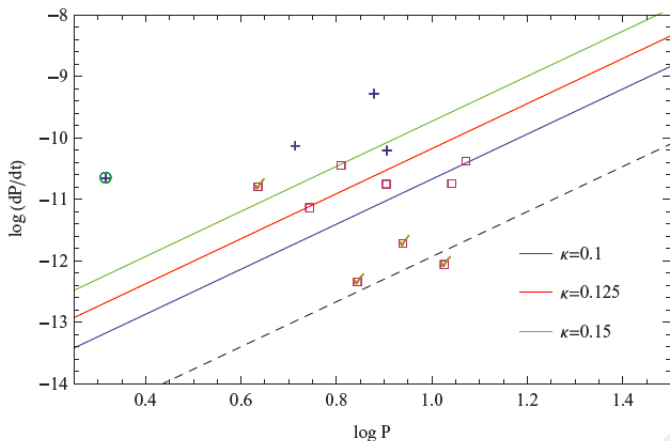
$$B_0 \gtrsim \left( \frac{\kappa}{f(1)} \right) \left( \frac{P}{1\text{s}} \right)^{7/3} \left( \frac{R_s}{10\text{km}} \right)^{-3} 10^{12}\text{G} ,$$

which gives the expression for the death-line of the magnetars in the form

$$\log \dot{P} = \frac{11}{3} \log P - 15.6 - 2 \log \left( \frac{\kappa}{f(1)} \right) - 6 \log \left( \frac{R_s}{10\text{km}} \right) .$$



Death-lines for the aligned magnetar for different values of the parameter  $\kappa$ . The dashed line indicates the position of the Newtonian death-line. Crosses and squares indicate the position of SGRs and AXPs, respectively. AXPs from which the radio emission has been registered are marked with ticks, radio-loud soft gamma-ray repeater is enclosed in circle.



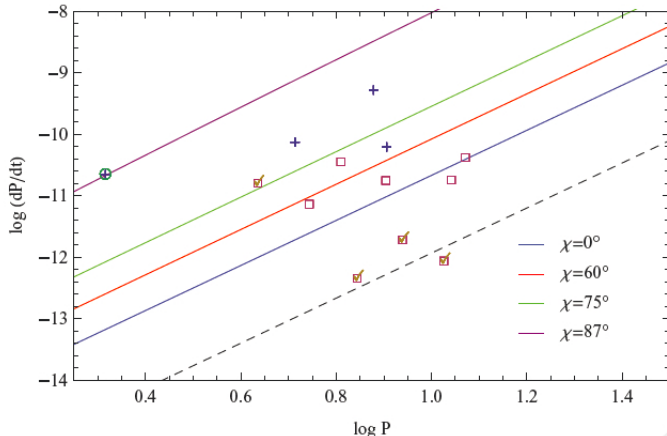
# Dependence of death-lines from inclination angle $\chi$

The expression for the death-line of the inclined magnetar is

$$B > 2^{-\frac{8}{3}} 3 \xi_{min}^{-\frac{2}{3}} \left\{ \left| \frac{\kappa}{f(1)} \cos \chi (1 - \xi_{min}^2) + \frac{3}{4} \frac{1}{(f(1))^{3/2}} \sqrt{\frac{R_s}{R_c}} \left( \frac{\Theta(\eta)}{\Theta_0} - H(1) \right) \sin \chi \right| \right\}^{-1} \left( \frac{P}{1s} \right)^{\frac{7}{3}} \left( \frac{R_s}{10km} \right)^{-3} 10^{12} \text{G}.$$



Death-lines for the misaligned magnetar for different values of the inclination angle  $\chi$ . The value of  $\kappa$  is taken to be 0.1. The dashed line indicates the position of the Newtonian death-line. Crosses and squares indicate the position of SGRs and AXPs, respectively. Anomalous X-ray pulsars from which the radio emission has been registered are marked with ticks, radio-loud soft gamma-ray repeater is enclosed in circle.



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# EM scalar potential

GR EM scalar potential in the polar cap region of rotating and oscillating aligned magnetar magnetosphere is given by

$$\Psi(\theta, \phi) = \frac{B_0}{2} \frac{R_s^3}{R_c^2} \frac{\kappa}{f(1)} (1 - \xi^2) - e^{-i\omega t} \tilde{\eta}(R_s) B_0 R_s \sum_{l=0}^{\infty} \sum_{m=-l}^l Y_{lm}(\theta, \phi) .$$

The condition for radio emission on the intensity of MF is given by

$$B > 2^{-\frac{1}{3}} 6\pi \left\{ \int_0^{2\pi} \xi_{min}^{2/3} \left| \frac{\kappa}{f(1)} (1 - \xi_{min}^2) - 2 \frac{\tilde{\eta}(R_s)}{f^m(1)} \left( \frac{R_s}{R_c} \right)^{\frac{m}{2}-2} \xi_{min}^m A_{lm}(\phi) \right| d\phi \right\}^{-1} \times \left( \frac{P}{1s} \right)^{\frac{7}{3}} \left( \frac{R_s}{10km} \right)^{-3} 10^{12} \text{G} ,$$

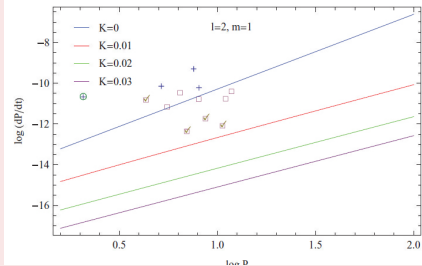
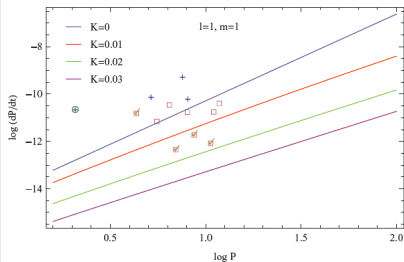
in the approximation  $Y_{lm}(\theta, \phi) \approx A_{lm}(\phi) \theta^m$  being valid in the limit of small polar angles  $\theta$ .

# Dependence of death-lines from parameter $K$

The amplitude of the oscillation is now parametrized in terms of the small number  $K = \tilde{\eta}(1)/\Omega R$ , giving the ratio between the velocity of oscillations and the linear rotational velocity of magnetar. The death-lines for rotating as well as oscillating magnetars for two modes of oscillations and different values of the parameter  $K$  are provided.



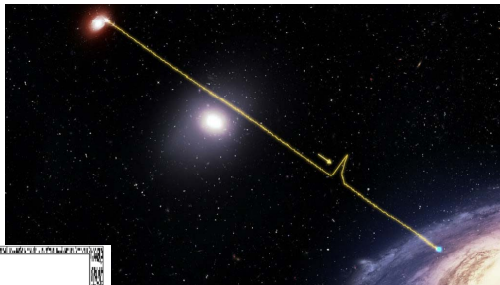
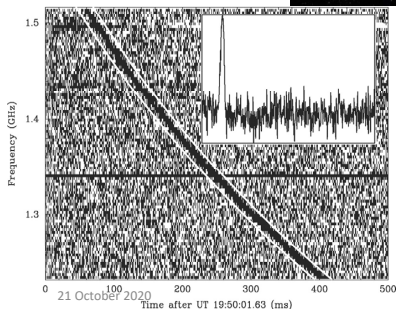
Death-lines for rotating and oscillating magnetars in the  $P - \dot{P}$  diagram. The left panel corresponds to the mode (1, 1) and values of  $K = 0, 0.01, 0.02, 0.03$ . The right panel corresponds to the mode (2, 1) and values of  $K = 0, 0.01, 0.02, 0.03$ . Other parameters are taken to be  $R_s = 10\text{km}$ ,  $M = 2M_\odot$  and  $\kappa = 0.15$ . Crosses and squares indicate the position of SGRs and AXPs, respectively. AXPs from which the radio emission has been registered are marked with ticks, radio-loud soft gamma-ray repeater is enclosed in circle.



# Fast Radio Bursts (FRBs)

D.Lorimer, D. Narkevic  
Nature 2007

“Lorimer” bursts



Quasi-periodically Repeating FRBs

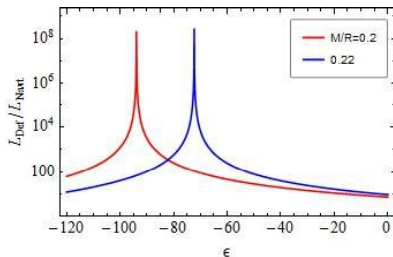
K M Rajwade et al **Possible periodic activity in the repeating FRB 121102**, MNRAS 2020  
( $P = 10\text{--}150$  days) **600MHz–8GHz** ( $4 \div 50$  cm)

**Periodic activity from a fast radio burst source**  
(The CHIME/FRB Collaboration\*) Nature 2020  
( $P = 16.35 \pm 0.15$  days) **400–800MHz** ( $40 \div 75$  cm)

10

# Radiation luminosity

## Plasma magnetospheric radiations

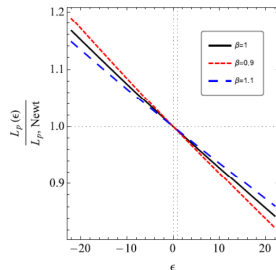


$$L_{\text{Newt}} \cong 10^{38} \text{ erg/sec}$$

$$L_{\text{max}} \cong 10^{47} \text{ erg/sec}$$

one may fit the time dependence of the source NS deformation using recorded data of appearance of a repeating FRB

## Magnetodipolar radiations



Wenbin & Kumar, MNRAS Letters, 483,1 (2019)

$$L_{\text{max}} \cong 2 \times 10^{47} \text{ erg/sec}$$

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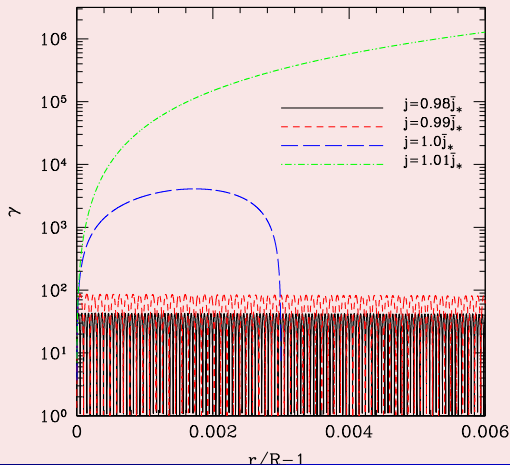
Existing models for the drifting subpulses

Our results in frame of the space charge limited flow model

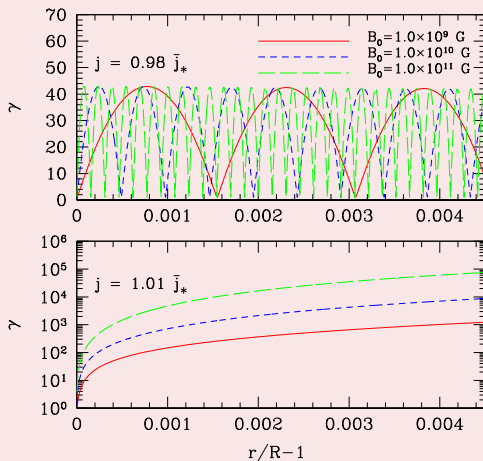
## 5 Conclusion



Dependence of the Lorentz factor on the ratio  $j/\bar{j}_*$  for a neutron star with  $M = 1.4M_\odot$ ,  $R = 10$  km,  $P = 0.1$  s,  $\chi = 30^\circ$ ,  $B_0 = 1.0 \times 10^{12}$  G,  $\theta_* = 0^\circ$ ,  $\Theta_0 = 2^\circ$ ,  $\gamma_* = 1.01$ .

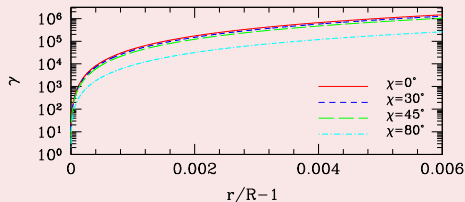


Lorentz factor dependence on the intensity of the magnetic field for a neutron star with  $M = 1.4M_\odot$ ,  $R = 10$  km,  $P = 0.1$  s,  $\chi = 30^\circ$ ,  $\theta_* = 0^\circ$ ,  $\Theta_0 = 2^\circ$ ,  $\gamma_* = 1.01$ . Top panel:  $j = 0.98\bar{j}_*$ . Bottom panel:  $j = 1.01\bar{j}_*$ .

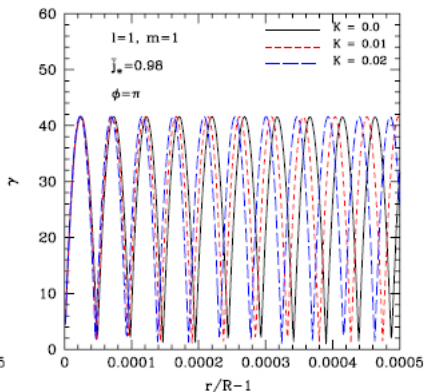
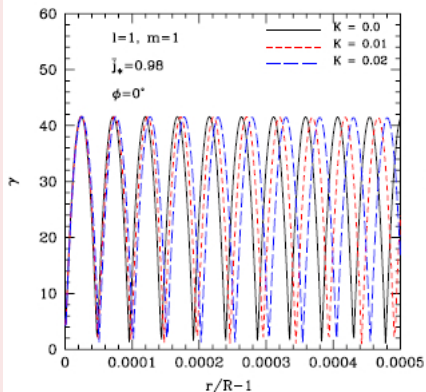




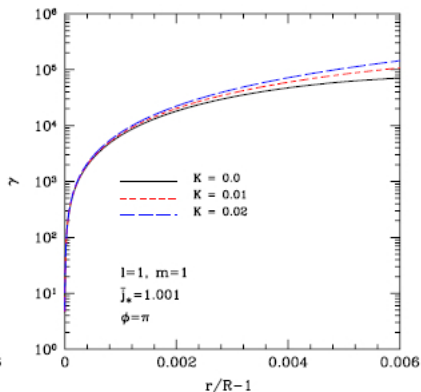
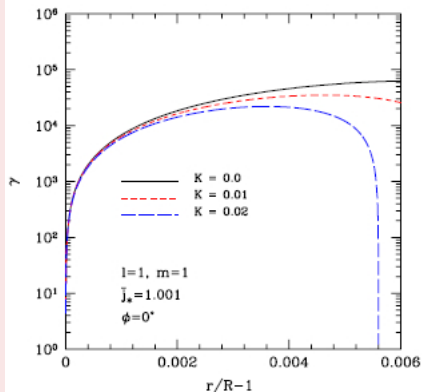
Lorentz factor dependence on the inclination angle  $\chi$  for a neutron star with  $M = 1.4M_\odot$ ,  $R = 10$  km, and  $P = 0.1$  s,  $j = 1.01\bar{j}_*$ ,  $\theta_* = 0^\circ$ ,  $\Theta_0 = 2^\circ$ ,  $\gamma_* = 1.01$ ,  $B_0 = 1.0 \times 10^{12}$  G. The Lorentz factor decreases for larger inclination angles.



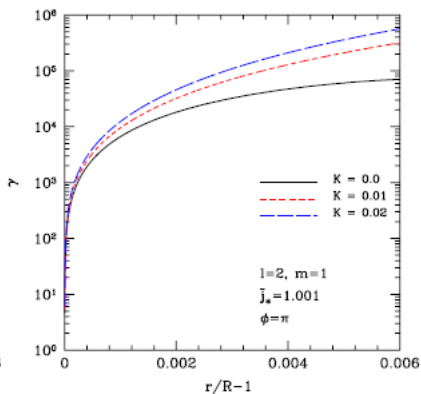
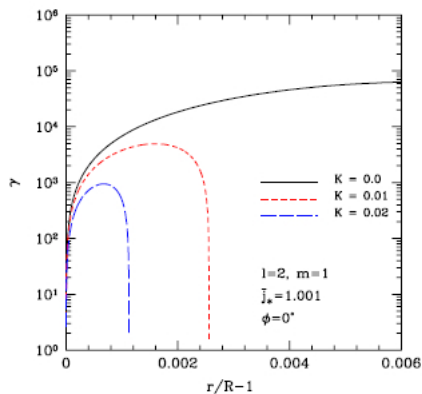
Lorentz factor dependence on the normalized amplitude of the stellar oscillations  $K$  for the mode of oscillations  $(l, m) = (1, 1)$  with  $\theta_* = 2^\circ$ ,  $\Theta_0 = 3^\circ$ ,  $\gamma_* = 1.015$ ,  $B_0 = 1.0 \times 10^{12} \text{G}$  for the case  $j = 0.98 \bar{j}_*$ . The left panels show the solution for  $\phi = 0$ , the right panels for  $\phi = \pi$ .



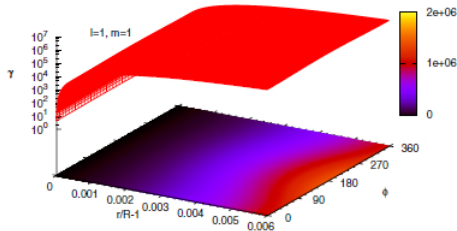
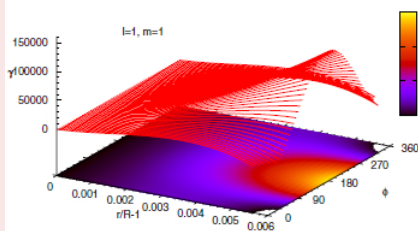
Lorentz factor dependence on the normalized amplitude of the stellar oscillations  $K$  for the mode of oscillations  $(l, m) = (1, 1)$  with  $\theta_* = 2^\circ$ ,  $\Theta_0 = 3^\circ$ ,  $\gamma_* = 1.015$ ,  $B_0 = 1.0 \times 10^{12} \text{ G}$  for the case  $j = 1.001 \bar{j}_*$ . The left panels show the solution for  $\phi = 0$ , the right panels for  $\phi = \pi$ .



Lorentz factor dependence on the normalized amplitude of the stellar oscillations  $K$  for the mode of oscillations  $(l, m) = (2, 1)$  with  $\theta_* = 2^\circ$ ,  $\Theta_0 = 3^\circ$ ,  $\gamma_* = 1.015$ ,  $B_0 = 1.0 \times 10^{12} \text{G}$ . The two panels correspond to the case  $j = 1.001 \bar{j}_*$ . The left panel shows the solution for  $\phi = 0$ , the right panel for  $\phi = \pi$



Lorentz factor as a function of radial distance and azimuthal angle  $\phi$  for a model with stellar oscillations  $K = 0.02$ ,  $(l, m) = (1, 1)$ ,  $\theta_* = 2^\circ$ ,  $\Theta_0 = 3^\circ$ ,  $\gamma_* = 1.015$ ,  $B_0 = 1.0 \times 10^{12} \text{G}$ . Left panel:  $j = 1.001 \bar{j}_*$ . Right panel:  $j = 1.01 \bar{j}_*$ .



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# Drifting Subpulses as a Tool for Studies of Pulsar Magnetosphere

- Phenomena of drifting subpulses
- Existing models for the drifting subpulses
- Our results in frame of the space charge limited flow model

V.S. Morozova, Ahmedov B.J., O. Zanotti, Explaining the subpulse drift velocity of pulsar magnetosphere within the space-charge limited flow model, **MNRAS**, 2014, V. 444, 1144



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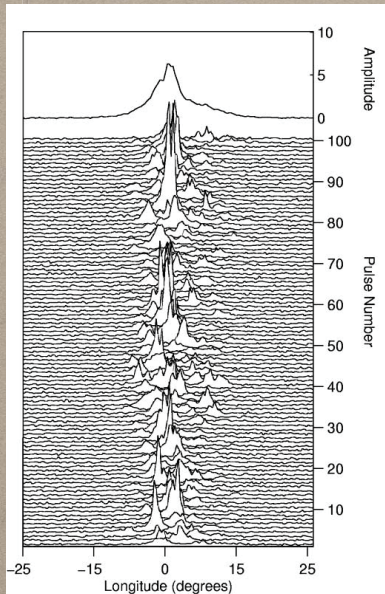
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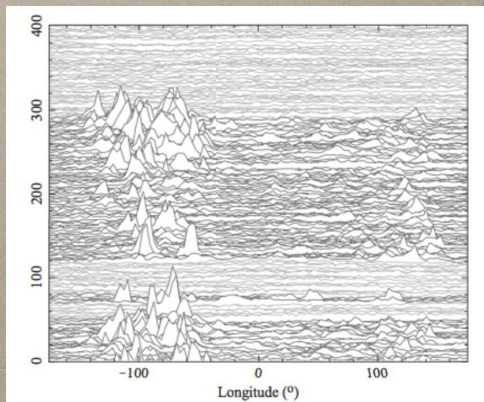




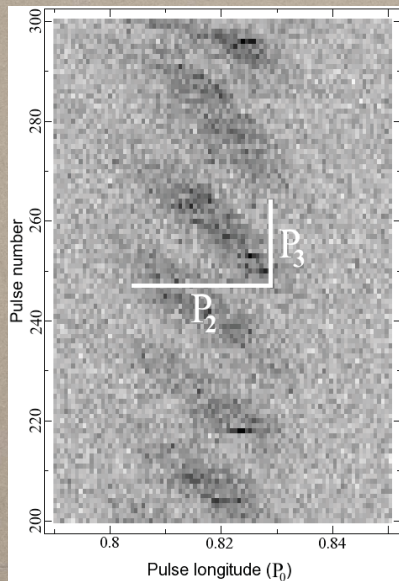
## Drifting subpulses



- \* Average pulse profile is very stable and represents a unique "fingerprint" of a given pulsar
- \* Subsequent pulses plotted on top of each other show rich microstructure



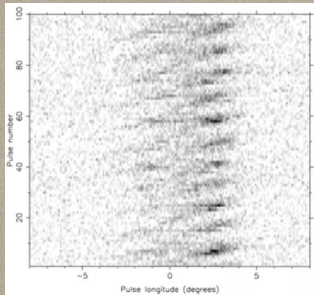
## Drifting subpulses



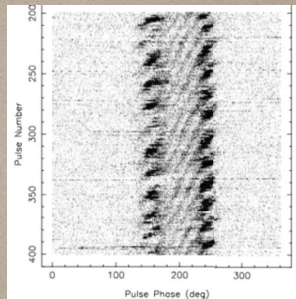
*Subpulse drift velocity*

$$\omega_D = \frac{P_2}{P_3}$$

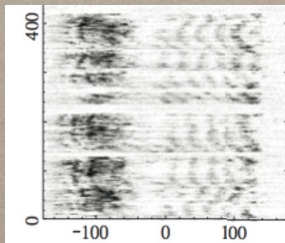
## Various subpulse behavior



PSR B0320+39 from R. T. Edwards et al. (2003)



PSR B0818-41 from B. Bhattacharyya et al. (2007)



PSR B0826-34 from van Leeuwen & Timokhin (2012)



PSR J0815-09 from Qiao et al. (2004)

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*How many charged particles will actually leave the surface of the star?*

*A. All required for the screening of the induced electric field*

Arons & Scharlemann (1979)

**Space-charge limited flow (SCLF) model**

*B. None*

Ruderman & Sutherland (1975)

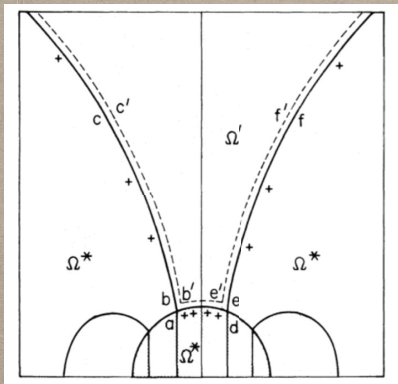
**Vacuum gap model**

*C. Some part of the amount required for the screening*

Gil & Sendyk (2000)

**Partially screened gap model**

## Vacuum gap model



- \* A vacuum gap will be formed close to the surface of the star
- \* The gap will periodically discharge in the form of sparks
- \* Sparks are assumed to be responsible for the appearance of the drifting subpulses

$$\omega_D = \frac{\Delta V}{B_s r_p} c$$

potential drop of the gap

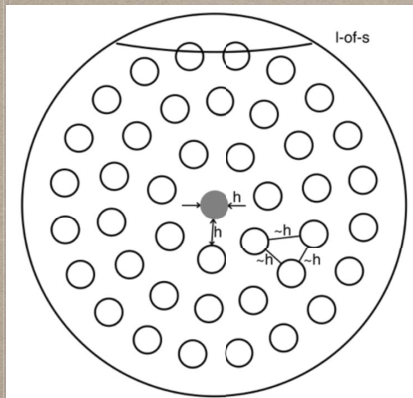
surface magnetic field

radius of the polar cap

*Predicted velocities are too large in comparison with the observed*



## Partially screened gap model



- \* *Even when the vacuum gap is screened on  $\sim 95\%$ , the remaining potential drop is enough for the spark discharges to appear*
- \* *Sparks are assumed to densely populate the polar cap region*

*Predicted velocities can be brought to correspondence with the observed ones, but the degree of screening (shielding factor) is fine tuned and different for different pulsars*

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## SCLF model

- \* *Scalar potential is induced due to the difference between the actual charge density in the magnetosphere and the charge density needed to screen the accelerating electric field*

$$\Delta V = -4\pi(\rho - \rho_{GJ})$$

- \* *Provides analytical solutions for the charge density and electromagnetic field regions close to the surface and far from the surface of the neutron star*

***Was never used for the explanation of the drifting sub pulses:***

- *Potential drop is too small ( $10^9$  V vs  $10^{12}$  V)*
- *No place for the discharges*

## van Leeuwen & Timokhin (2012)

$$v_D = \frac{\Delta V}{B_s r_p} c \quad ?$$

$$\vec{v} = \frac{\vec{E} \times \vec{B}}{B^2} c$$

$$\vec{E} = -\nabla V$$

$$v_D = \frac{180^\circ}{\xi} \frac{dV}{d\xi}$$

$$\xi \equiv \frac{\theta}{\theta_{pc}}$$

The drift velocity is defined by the shape of the potential, not by its absolute value

*What if we try to check the SCLF model?*

## Expression for the plasma velocity

$$\omega_{D \text{ low}} = \frac{180^\circ}{\xi} \frac{12\sqrt{1-\varepsilon}\Theta_0}{\bar{r}} \left\{ -2\kappa \cos \chi \sum_{i=1}^{\infty} \left[ \exp \left( \frac{k_i(1-\bar{r})}{\Theta_0\sqrt{1-\varepsilon}} \right) - 1 + \frac{k_i(\bar{r}-1)}{\Theta_0\sqrt{1-\varepsilon}} \right] \frac{J_1(k_i\xi)}{k_i^3 J_1(k_i)} \right. \\ \left. + \Theta_0 H(1)\delta(1) \sin \chi \cos \phi \sum_{i=1}^{\infty} \left[ \exp \left( \frac{\tilde{k}_i(1-\bar{r})}{\Theta_0\sqrt{1-\varepsilon}} \right) - 1 + \frac{\tilde{k}_i(\bar{r}-1)}{\Theta_0\sqrt{1-\varepsilon}} \right] \frac{J_0(\tilde{k}_i\xi) - J_2(\tilde{k}_i\xi)}{2\tilde{k}_i^3 J_2(\tilde{k}_i)} \right\}$$

$$\bar{r} \equiv \frac{r}{R} \quad \xi \equiv \frac{\theta}{\theta_{pc}} \quad \phi \quad - \text{ spherical coordinates}$$

- \* *Are the values of drift velocity predicted by this expression compatible with the observed subpulse velocities?*
- \* *May the angular dependence of the drift velocity help in explaining the longitudinal subpulse behavior?*

## Comparison with the pulsar data

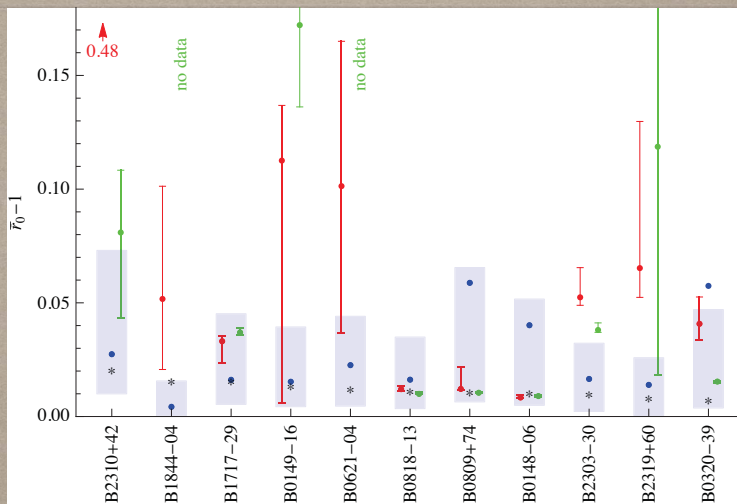
- \* *Weltevrede et al. (2006), (2007) did the first systematic study of the subpulse behavior of large amount of pulsars (at 21 cm and 92 cm observational wavelength)*
- \* *From 187 pulsars more than 55 % show the subpulse phenomena (revealed by the spectral methods)*
- \* *We chose 13 pulsars with known observing geometry (the inclination angle  $\chi$ )*

$$\omega_D = \omega_D(\bar{r}, \xi, \phi)$$

$$\xi = 0.9, \quad \phi = \pi$$

*Find  $\bar{r}$  so that  $\omega_D(\bar{r}) = \omega_{observed}$*

- \* *One pulsar does not have a solution, one has the opposite drift sense at two observing frequencies*



Red data points correspond to the observing wavelength at 21 cm

Green data points correspond to the observing wavelength at 92 cm

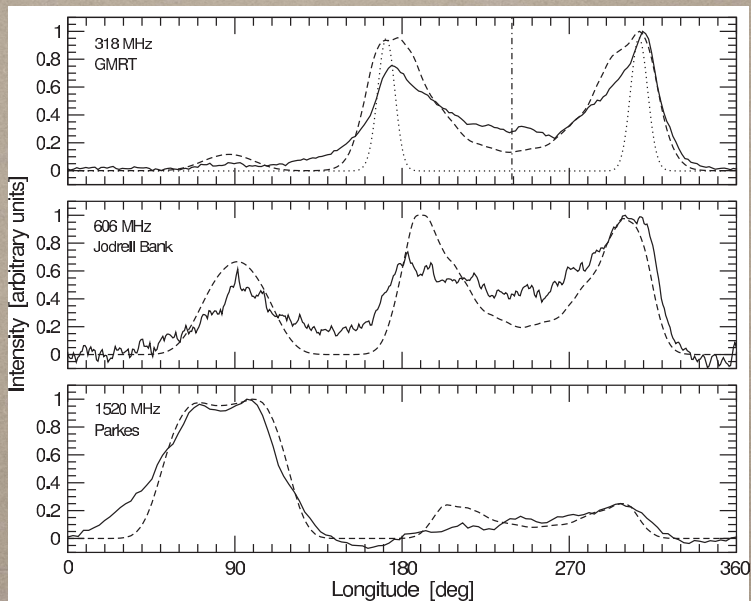
Blue shadowed rectangles and blue points indicate the pair formation front (PFF)

## Pair formation front

- \* *Primary particles, emitted from the surface, accelerate in the inner magnetosphere and emit high energy gamma photons via:*
  - *Curvature radiation*
  - *Inverse Compton scattering*
- \* *Emitted gamma photons produce electron-positron pairs in the background magnetic field*
- \* *Pair production leads to the screening of the accelerating electric field and prevents further acceleration above the pair formation front*

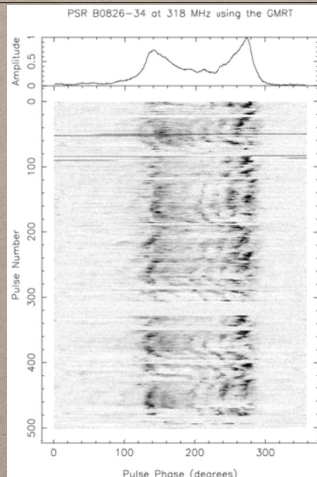


## PSR B0826-34



## PSR B0826-34

| Observing frequency (MHz) | Measured drift velocity ( $^{\circ}/P$ ) | Reference                     | Average drift velocity ( $^{\circ}/P$ ) |
|---------------------------|--|-------------------------------|---|
| 318                       | $-0.8 \div 1.9$                          | Gupta et al. (2004)           | 0.55                                    |
| 645                       | $-1.5 \div 2.1$                          | Biggs et al. (1985)           | 0.3                                     |
| 1374                      | $-3.2 \div 3.6$                          | Esamdin et al. (2005)         | 0.2                                     |
| 1374                      | $-1 \div 1.5$                            | van Leeuwen & Timokhin (2012) | 0.25                                    |



*Measured subpulse separation*

$$P_2 = 24.9^{\circ} \pm 0.8^{\circ}$$

*The pulsar is almost aligned, our  
model predicts negative drift  
velocity*

*What if the positive average drift is  
only apparent?*

$$\omega_D = (0.55^{\circ} - 24.9^{\circ})/P = -24.35^{\circ}?$$

$$P_3 \approx P \quad ?$$



## Our model for the observing geometry

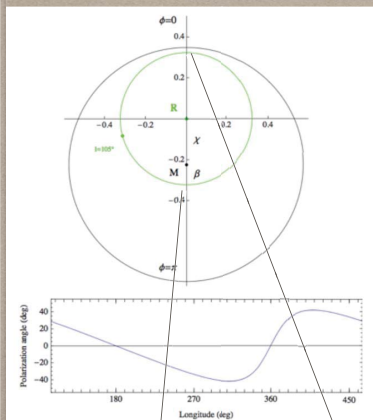
*Black circle - boundary of the polar cap (0.57 deg)*

*Green circle - line of sight of the observer*

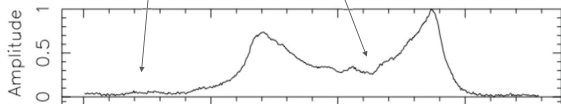
$$\chi = 0.225^\circ$$

$$\beta = 0.098^\circ$$

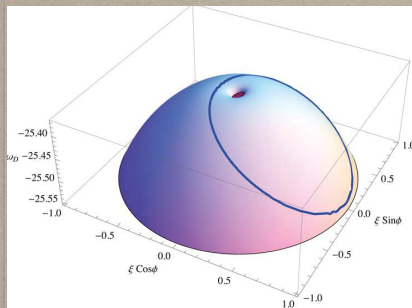
*Consistent with the polarization data and with the width of the profile*



PSR B0826-34 at 318 MHz using the GMRT

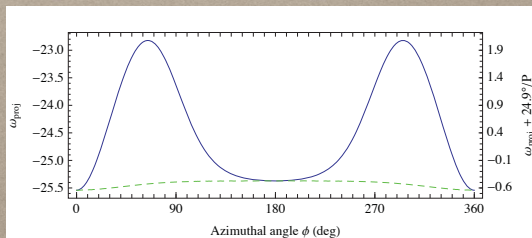


## Explaining the range of measured velocities

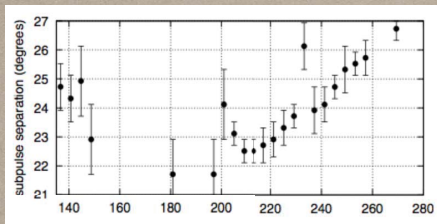


\* Plasma drift velocity across the pulsar polar cap in the SCLF model

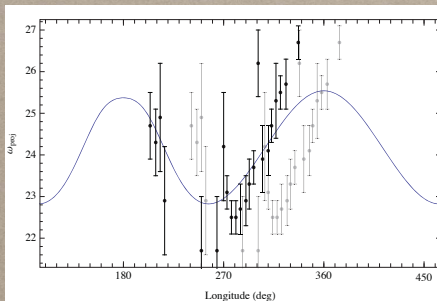
$$\vec{\omega}_{proj} = \frac{\vec{\omega}}{\sqrt{1 + \left(\frac{d\xi}{d\phi}\right)^2}}$$



# Explaining the longitudinal dependence of subpulse separation

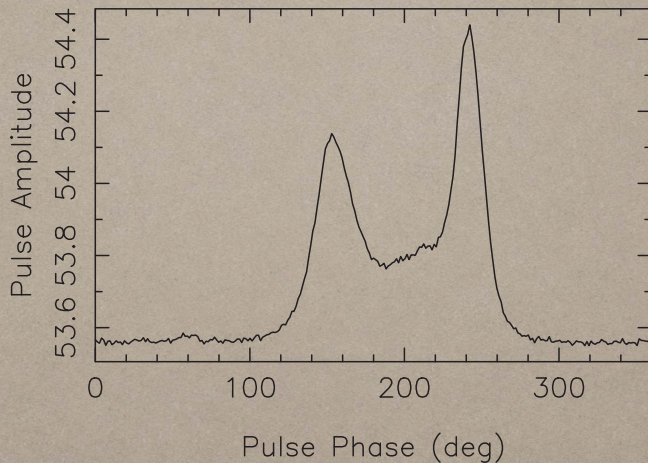


*Measured subpulse separation of B0826-34 from Gupta et al. (2004)*



*Black points represent the observed data (given in gray), shifted in order to get the visual correspondence*

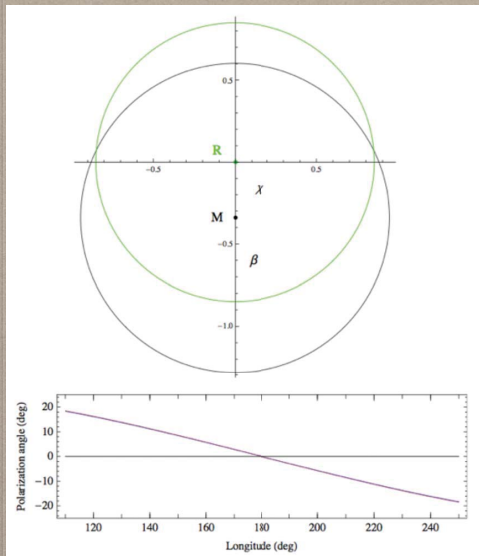
## PSR B0818-41



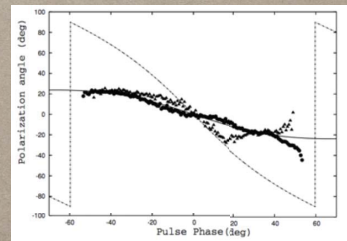
$$P = 0.545 \text{ sec}$$

$$B_s = 1.03 \times 10^{11} \text{ G}$$

## Our model for the observing geometry

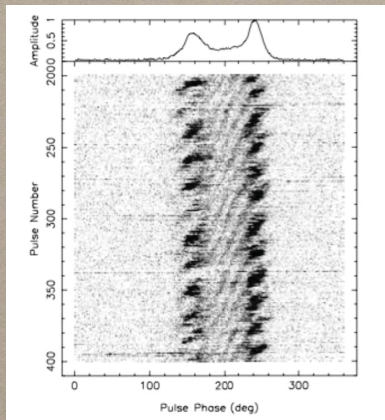


*Consistent with the  
polarization data  
and with the width  
of the profile*

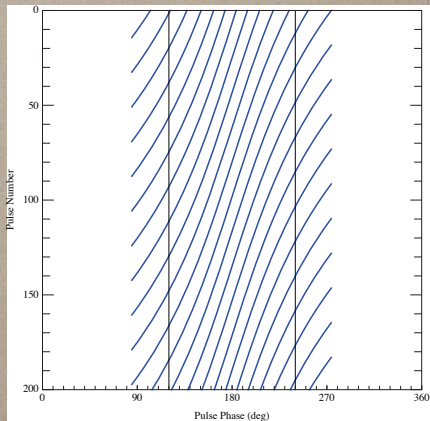


from Bhattacharyya et al. (2009)

## *Angular dependence of the drift velocity can account for the curved subpulse drift bands of B0818-41*



from Bhattacharyya et al. (2009)



obtained with our model

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## 3 Plasma magnetosphere of neutron stars in GR

Plasma MS of rotating and oscillating NSs in GR

GR magnetosphere of pulsar and Particle acceleration in a polar cap

Part time pulsars

Relativistic death line for magnetars

Death line for rotating and oscillating magnetars

Particle acceleration in NS magnetospheres

## 4 Subpulse drift velocity of pulsar magnetosphere within the space-charge limited flow model

Phenomena of drifting subpulses

Existing models for the drifting subpulses

Our results in frame of the space charge limited flow model

## 5 Conclusion



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- The dependence for the energy losses on the oscillating behavior reflects in useful relation between the product  $P\dot{P}$  and the amplitude of the stellar oscillation.
- A connection between the phenomenology of intermittent pulsars, characterized by the periodic transition from active to dead periods of radio emission in few observed sources, with the presence of an oscillating magnetosphere. During the active state, star oscillations may create relativistic wind of charged particles by virtue of the additional accelerating electric field. After a timescale of the order of tens of days stellar oscillations are damped, and the pulsar shifts below the death line in the  $P - B$  diagram, thus entering the OFF invisible state of intermittent pulsars.





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- A detailed analysis of the position of the death-line in the  $P - \dot{P}$  diagram for a magnetar is performed. When the compactness of the neutron star is increased, the death line shifts upwards in the  $P - \dot{P}$  diagram, pushing the magnetar in the radio-quiet region.
- When the inclination angle  $\chi$  between the angular momentum vector and magnetic moment is increased, the death-line shifts upwards in the  $P - \dot{P}$  diagram, pushing the magnetar in the radioquiet region.
- Larger compactness parameters of the star as well as larger inclination angles between the rotation axis and the magnetic moment produce death-lines well above the majority of known magnetars. This is consistent with the observational evidence of no regular radio emission from the magnetars in the frequency range typical for the ordinary pulsars.



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- The SCLF model predicts the subpulse drift velocities compatible to the observed ones at heights above the surface of the star close to the pair formation front
- The angular dependence of the plasma drift velocity in the SCLF model provides a natural explanation for the variation of the subpulse separation along the pulse
- In particular it may explain the curved subpulse driftbands of PSR B0818-41 and the range of the observed drift velocities of PSR B0826-34



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# Thank You

